Math 261 Exam 2 - Practice Problems

1. Find the derivative  $y' = \frac{dy}{dx}$  for each of the following:

(a) 
$$y = e^{2}x + ex^{2}$$
  
(b)  $y = \cot x$   
(c)  $y = \sqrt{x} \sec(x^{2})$   
(d)  $y = 2 \tan^{3}(2x^{3})$   
(e)  $y = \frac{x^{2} - 7\cos(3x)}{x + \sin(3 - 2x)}$   
(f)  $x^{2}y + 3xy - 5y^{2} = 7$   
(g)  $\cos^{2}(xy) = 1$ 

2. Use the formal limit definition of the derivative to find the derivative of the following:

(a) 
$$f(x) = x^2 - 3x$$
  
(b)  $f(x) = \frac{2}{x-3}$   
(c)  $f(x) = \sqrt{x-2}$ 

- 3. Use the quotient rule to derive the formula for the derivative of tan(x).
- 4. If  $f(x) = \sqrt{3x-5}$ , find the intervals where f(x) is continuous, and find the intervals where f(x) is differentiable.
- 5. If  $f(x) = 3x^4 5x^2 + 7x 12$ , use differentials to approximate f(1.1)
- 6. Use differentials to estimate  $\sqrt[3]{9}$ . How good is your estimate?
- 7. Suppose helium is being pumped into a spherical baloon at a rate of 4 cubic feet per minute. Find the rate at which the radius is changing when the radius is 2 feet.
- 8. Find the equation of the tangent line to the graph of  $f(x) = \tan(4x)$  when  $x = \frac{3\pi}{16}$
- 9. Find the points on the graph of  $y = 2x^3 + 3x^2 72x + 5$  at which the tangent line is horizontal.
- 10. Find the equation of the tangent line to the graph of the relation  $x^3 + x^2y = \sqrt{y^3} 3$  at the point (1, 4).
- 11. Draw the graph of a function f(x) that is continuous when x = 3, but is not differentiable when x = 3.
- 12. Find g'(2) if h(x) = f(g(x)), f(3) = -2, g(2) = 3, f'(3) = 5, and h'(2) = -30.
- 13. Find  $f^{(8)}(x)$  if  $f(x) = \sin(2x)$
- 14. Find  $f^{(13)}(x)$  if  $f(x) = x^{12} + 7x^5 3x^3 1$