

1. Suppose you throw a ball vertically upward. If you release the ball 7 feet above the ground at an initial speed of 48 feet per second, how high will the ball travel? (Assume gravity is  $-32ft/sec^2$ )
2. Use Newton's Method to approximate a real root of the function  $f(x) = x^3 - 5x^2 + 27$  to 5 decimal places.
3. Use Newton's Method to approximate  $\sqrt{10}$  to 5 decimal places.
4. Find each of the following indefinite integrals:

(a)  $\int \frac{x^{\frac{3}{2}} - 7x^{\frac{1}{2}} + 3}{x^{\frac{1}{2}}} dx$

(b)  $\int \sin^3 x \cos x dx$

(c)  $\int 5x(x^2 + 1)^8 dx$

(d)  $\int \frac{x}{\sqrt{x+1}} dx$

5. Solve the following differential equations under the given initial conditions:

(a)  $\frac{dy}{dx} = \sin x + x^2; y = 5$  when  $x = 0$

(b)  $g''(x) = 4 \sin(2x) - \cos(x); g'(\frac{\pi}{2}) = 3; g(\frac{\pi}{2}) = 6$

6. Express the following in summation notation:

(a)  $2 + 5 + 10 + 17 + 26 + 37$

(b)  $x^2 + \frac{x^3}{4} + \frac{x^4}{9} + \dots + \frac{x^{11}}{100}$

7. Evaluate the following sums:

(a)  $\sum_{k=2}^5 k^2(k+1)$

(b)  $\sum_{k=3}^{20} k^3 - k^2$

8. Express the following sums in terms of  $n$ :

(a)  $\sum_{k=1}^n 3k^2 - 2k + 10$

(b)  $\sum_{k=3}^n k(k^2 - 1)$

9. Consider  $f(x) = 3x^2 - 5$  in the interval  $[3, 7]$

- (a) Find a summation formula that gives an estimate the definite integral of  $f$  on  $[3, 7]$  using  $n$  equal width rectangles and using midpoints to give the height of each rectangle. You do not have to evaluate the sum or find the exact area.
- (b) Find the norm of the partition  $P : 3 < 3.5 < 5 < 6 < 6.25 < 7$
- (c) Find the approximation of the definite integral of  $f$  on  $[3, 7]$  using the Riemann sum for the partition  $P$  given in part (b).

10. Assume  $f$  is continuous on  $[-5, 3]$ ,  $\int_{-5}^{-1} f(x) dx = -7$ ,  $\int_{-1}^3 f(x) dx = 4$ , and  $\int_1^3 f(x) dx = 2$ . Find:

(a)  $\int_3^{-1} f(x) dx$

(b)  $\int_{-5}^1 f(x) dx$

(c)  $\int_{-5}^3 f(x) dx$

(d)  $\int_{-1}^{-1} f(x) dx$

(e) Find the average value of  $f$  on  $[-5, -1]$

11. Evaluate the following:

(a)  $\int_1^4 x^3 + \frac{1}{\sqrt{x}} + 2 dx$

(b)  $\int_0^1 x^2(2x^3 + 1)^2 dx$

(c)  $\int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \sin^3(2x) \cos(2x) dx$

(d)  $\int_{-\pi}^{\pi} \sin x dx$

(e)  $\frac{d}{dx} \left( \int_1^3 t\sqrt{t^2 - 1} dt \right)$

(f)  $\int_1^3 \left[ \frac{d}{dx} \left( t\sqrt{t^2 - 1} \right) dt \right]$

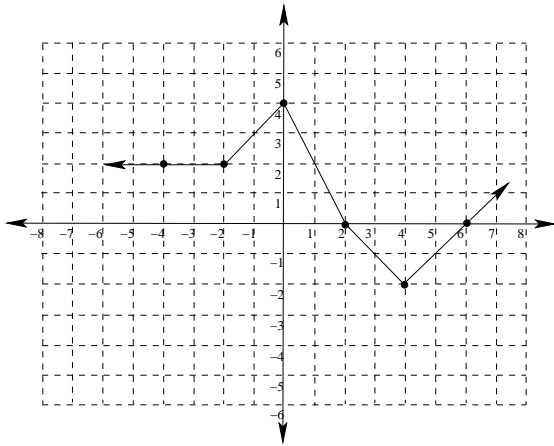
12. Suppose  $G(x) = \int_2^x \frac{1}{t^2 + 1} dt$

(a) Find  $G'(2)$

(b) Find  $G'(x^2)$

(c) Find  $G''(3)$

13. Given the following graph of  $f(x)$  and the fact that  $G(x) = \int_{-2}^x f(t) dt$ :



- (a) Find  $G(6)$   
(b) Find  $G'(6)$   
(c) Find  $G''(6)$
14. (a) Use the Trapezoidal Rule with  $n = 4$  to approximate  $\int_0^4 2x^3 dx$   
(b) Find the maximum possible error in your approximation from part (a).  
(c) Use the Fundamental Theorem of Calculus to find  $\int_0^4 2x^3 dx$  exactly. How far off was your estimate? How does the actual error compare to the maximum possible error?