1. Evaluate each of the following integrals:.

(a)
$$\int xe^{4x} dx$$

(b)
$$\int e^{3x} \cos(8x) \ dx$$

(c)
$$\int x \sec^2 x \ dx$$

(d)
$$\int x \sec(x^2) \ dx$$

(e)
$$\int x5^x dx$$

(f)
$$\int e^{\sqrt{x}} dx$$

(g)
$$\int \sec^3 x \ dx$$

(h)
$$\int \sin(\ln x) \ dx$$

(i)
$$\int x^3(x^2+5)^{49} dx$$

(j)
$$\int x^2(x^3+5)^{49} dx$$

2. Derive the following reduction formula:

$$\int \cos^{n} x \ dx = \frac{1}{n} \cos^{n-1} x \sin x + \frac{n-1}{n} \int \cos^{n-2} x \ dx$$

3. Find the volume of the solid generated by revolving the region in the first quadrant bounded by the coordinate axes, the curve $y = e^{-x}$, and the line x = 1 about the line x = 1