Let f(x) = -ln(1 - x).
 (a) Find f'(x), f''(x), f'''(x), f⁽⁴⁾(x), and f⁽ⁿ⁾(x)

(b) Find $f'(0), f''(0), f'''(0), f^{(4)}(0)$, and $f^{(n)}(0)$

- (c) Find the *n*th-degree Maclaurin polynomial of f
- (d) Find the Maclaurin series for f(x). (Do not verify that $\lim_{n\to\infty} R_n(x) = 0$
- (e) Find the interval of convergence for this Maclaurin series.

- 2. Find the first five terms of the Taylor series for the following functions at a given value c:
 - (a) $f(x) = \cos x$ at $c = \frac{\pi}{3}$

(b) $f(x) = \sqrt{x}$ at c = 4

3. Find the Maclaurin series for $f(x) = 6x^4 - 2x^3 + 4x^2 + x + 7$. Show all work!

4. Find the sum of each of the following infinite series. Give exact answers.

Name:

(a)
$$1 - \frac{1}{2!} + \frac{1}{4!} - \frac{1}{6!} + \dots + (-1)^n \frac{1}{(2n)!} + \dots$$

(b)
$$1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \dots + (-1)^n \frac{1}{n+1} + \dots$$

(c)
$$\frac{\pi}{6} - \frac{\pi^3}{6^3 \cdot 3!} + \frac{\pi^5}{6^5 \cdot 5!} - \dots + (-1)^n \frac{\pi^{2n+1}}{6^{2n+1}(2n+1)!} + \dots$$

5. Find the Indicated Taylor polynomial and remainder given f, c and n:

(a)
$$f(x) = \cos x, \ c = \frac{\pi}{4}, \ n = 4$$

(b)
$$f(x) = \frac{1}{(x-3)^2}, c = 4, n = 5$$

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6. If we used problem 6(a) to approximate $\cos 47^{\circ}$, what decimal place accuracy could we achieve?

7. (a) Use problem 6(b) to approximate $\frac{1}{(.9)^2}$

(b) Use the Taylor remainder in problem 6(b) to estimate the error in this approximation.

8. Determine the number of decimal places of accuracy that the given approximation formula yields for $|x| \leq 0.1$.

(a)
$$e^x \approx 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4$$

(b)
$$\sin x \approx x - \frac{1}{6}x^3 + \frac{1}{120}x^5$$

(c)
$$\ln(1+x) \approx x - \frac{1}{2}x^2 + \frac{1}{3}x^3 - \frac{1}{4}x^4$$