1. Evaluate each of the following integrals:.

(a) 
$$\int x e^{4x} dx$$

(b) 
$$\int e^{3x} \cos(8x) dx$$

(c) 
$$\int x \sec^2 x \, dx$$

(d) 
$$\int x \sec(x^2) dx$$

(f) 
$$\int e^{\sqrt{x}} dx$$

(g) 
$$\int \sec^3 x \, dx$$

(h) 
$$\int \sin(\ln x) dx$$

(i) 
$$\int x^3 (x^2 + 5)^{49} dx$$

(j) 
$$\int x^2 (x^3 + 5)^{49} dx$$

2. Derive the following reduction formula:

$$\int \cos^n x \, dx = \frac{1}{n} \cos^{n-1} x \sin x + \frac{n-1}{n} \int \cos^{n-2} x \, dx$$

3. Find the volume of the solid generated by revolving the region in the first quadrant bounded by the coordinate axes, the curve  $y = e^{-x}$ , and the line x = 1 about the line x = 1