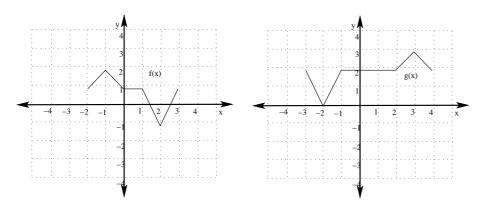
Exam 3 Practice Problems

- 1. True or False:
 - (a) Any two distinct points in the plane determine exactly one line.
 - (b) Any line can be written in the form y = mx + b.
 - (c) The graph of any circle is symmetric with respect to the origin.
 - (d) If a graph has two points with the same y-coordinate, then it is not the graph of a function y = f(x).
 - (e) Every function y = f(x) has at least one x-intercept.
- 2. Given the points A(2,-2) and B(-1,4):
 - (a) Find d(A, B)
 - (b) Find the midpoint of the line segment containing A and B.
 - (c) Find the equation for the line containing A and B in general form.
 - (d) Find the equation for the circle centered at B containing the point A.
 - (e) Find an equation for the vertical line containing B.
 - (f) Find an equation for the horizontal line containing A.
- 3. Find the equation for each line described below. Put your final answer in slope/intercept form.
 - (a) The line with slope 4 and y-intercept -7
 - (b) The line containing the points (-4,1) and (3,-7)
 - (c) The line parallel to the line 3x 4y = 12 passing through the point (1,3)
 - (d) The line perpendicular to the line 5y 2x = 3 and having x-intercept -1.
- 4. A 16oz jar of peanut butter cost \$1.78 in 1995. In 2005, a similar jar cost \$2.99.
 - (a) Find a line that models the price of peanut butter over time (hint: you can take x = 0 to represent 1995)
 - (b) Use your model to predict the price of peanut butter in 2010.
 - (c) According to your model, when will the price of peanut butter reach \$5.00 for a 16oz jar?
- 5. Given the graphs of f(x) and g(x) shown below, use graph transformations to graph each of the following. Label at least 3 points in your final graph.



(a) f(x) + 3

(d) g(2x)

(g) -f(-x) - 1

(b) g(x-2)

- (e) f(-x) + 1

(h) -2g(x+1)

(c) 2f(x) - 1

(f) $-\frac{1}{2}g(x)$

- 6. Find the equation for the each of the following circles. Then graph the circle.
 - (a) The circle with center (4, -5) and radius 6
 - (b) The circle with a diameter passing through the points (2, -2) and (-4, -2)
 - (c) The circle with center (2,1) and passing through the point (5,5)
- 7. Graph the circle with equation $x^2 + y^2 + 4x 6y 3 = 0$
- 8. Find the domain of the following functions (put your answers in interval notation):
 - (a) $f(x) = \frac{x^2 + x 2}{x^2 4}$
 - (b) $f(x) = \frac{\sqrt{4-2x}}{x^2-1}$
 - (c) $f(x) = \frac{4}{\sqrt{3x-5}}$
 - (d) $f(x) = \frac{\sqrt{3-2x}}{2x^2+x-15}$
- 9. Given that $f(x) = \sqrt{2x-2}$ and $g(x) = \frac{4}{3x-2}$
 - (a) Find $\frac{g}{f}(3)$
 - (b) Find $f \circ g(2)$
- 10. Given that $f(x) = \sqrt{3x-2}$ and $g(x) = x^2 4$
 - (a) Find $g \circ f(x)$
 - (b) Find $f \circ g(x)$
 - (c) Find the domain of $g \circ f(x)$. Give your answer in interval notation.
 - (d) Find the domain of $\frac{f}{g}$. Give your answer in interval notation.
- 11. An oil well off the Gulf Coast is leaking, with the leak spreading oil over the surface in the shape of a circle. At any time t, in minutes, after the beginning of the leak, the radius of the circular oil slick on the surface is r(t) = 4t feet. Let $A(r) = \pi r^2$ represent the area of the circle of radius r.
 - (a) Find $(A \circ r)(t)$
 - (b) Explain what $(A \circ r)(t)$ is in practical terms.
- 12. Given the tables below, find the following:

X	0	2	4	6	8
f(x)	1	5	8	4	0

X	0	2	4	6	8
g(x)	2	6	5	9	7

- (a) $\left(\frac{f}{g}\right)$ (8)
- (b) $(f \circ g)(2)$
- (c) $(g \circ g)(2)$
- (d) $f^{-1}(5)$
- (e) $f(g^{-1}(9))$
- 13. Determine whether or not the following functions are one-to-one. You must justify your answer to each part.
 - (a) f(x) = 3x 5
 - (b) $f(x) = x^3 x$
 - (c) f(x) = 3|x| 2
 - $(d) g(x) = -\frac{1}{2x}$

- 14. Use algebra to find the inverse of each of the following functions:
 - (a) f(x) = 5x 4
 - (b) $f(x) = \sqrt{x-4}$
 - (c) $f(x) = \frac{5x}{3-x}$
 - (d) $f(x) = \frac{2x-3}{3x+4}$
- 15. Solve the following systems of linear equations. Then graph the equations involved to show that your answer is reasonable.

 - (a) $\begin{cases} y = 3x 2\\ x + 2y = 5 \end{cases}$ (b) $\begin{cases} 3x 2y = 7\\ x + 2y = 5 \end{cases}$
 - (c) $\begin{cases} x 3y = 2 \\ 6y 2x = 5 \end{cases}$

 - (d) $\begin{cases} 5x 4y = 10 \\ 3x + 5y = 12 \end{cases}$ (e) $\begin{cases} x 2y = 5 \\ -2x + 4y = 10 \end{cases}$
- 16. Graph each of the following functions:
 - (a) $f(x) = 4^x$
 - (b) $f(x) = 5^{-x}$
 - (c) $f(x) = 2^x 1$
 - (d) $f(x) = 2^{x-1}$
- 17. Solve the following equations:
 - (a) $3^{2-3x} = 3^{2x+1}$
 - (b) $5^{4x} = 5^{3x-12}$
 - (c) $2^{5x+1} = 4^{3-2x}$
- 18. Suppose you have \$2,000 to invest.
 - (a) Find the amount you would have after 5 years if you deposit your \$2,000 in an account that pays 6% annual interest compounded monthly.
 - (b) Find the amount you would have after 5 years if you deposit your \$2,000 in an account that pays 4% annual interest compounded quarterly.
 - (c) Find the amount you would have after 5 years if you deposit your \$2,000 in an account that pays 5% annual interest compounded continuously.