

### Section 2.4: Error Analysis for Iterative Methods

- Know the definition of convergence of a sequence  $\{p_n\}_{n=0}^{\infty} \rightarrow p$  of **order**  $\alpha$  with **asymptotic error constant**  $\lambda$ . Also be able to apply it to find the order of convergence for a specific sequence, or to determine whether or not a given sequence is *linearly convergent* or *quadratically convergent*.
- Know the definition of a **root of multiplicity**  $m$  of a function  $f(x)$  and be able to find the multiplicity of a root  $p$  of a given function, and to express it in the form:  $f(x) = (x - p)^m \cdot q(x)$ .
- Understand the connection between a root  $p$  of multiplicity  $m$  and the value of derivatives of  $f$  evaluated at  $p$  as stated in Theorem 2.10
- Know and be able to apply the Modified Newton-Raphson Method to approximate a root of a function.

### Section 2.5: Accelerating Convergence

- Know the definition of the **forward difference operator**  $\Delta$
- Understand the and be able to Apply Aitken's method and Steffensen's Method to accelerate the convergence of Newton's Method.

### Section 2.6: Zeros of Polynomials and Muller's Method

- Know the definition of complex numbers and the basic properties of complex conjugates.
- Understand the definition of a polynomial, and know the statements of the Fundamental Theorem of Algebra, the Remainder Theorem, and the Factor Theorem.
- Know how to evaluate a polynomial function using synthetic division. Also be able to use synthetic division to find roots of a polynomial, to factor a polynomial, and to aid in carrying out Newton's Method.
- Be able to use Horner's method and deflation in order to find the real and complex roots of a polynomial function.
- Be able to use Muller's Method to find a root of a function. You do not need to memorize the formulas for  $a$ ,  $b$  and  $c$ . I will provide these if I ask a question on Muller's method.

### Section 3.1: Interpolation and the Lagrange Polynomial

- Understand the definition of interpolation and know the statement of the Weierstrass Approximation Theorem.
- Know the definition of the Kronecker  $\delta$  function.
- Know the definition of the Lagrange interpolating polynomial and be able to find the Lagrange interpolating polynomial to a function given the values of the function at  $n + 1$  distinct points.
- Know and be able to find the remainder term for a Lagrange interpolating polynomial and be able to use it to find an upper bound on the error of a particular approximation.
- Know the advantages and disadvantages of using Lagrange polynomials. In particular, remember that Lagrange polynomials lack permanence.

### Section 3.2 and 3.3: Divided Differences and Hermite Interpolation

- Know how to compute a divided difference table and be able to use it to find the Newton Divided Difference interpolating polynomial for a function given values of the function at  $n + 1$  distinct points.
- Know how to extend the method for computing Newton Divided Difference interpolating polynomials to cases where we know information about the derivatives of the original function at various points.
- Be able to extend the method for computing Newton Divided Difference interpolating polynomials to cases where the known values of the function are evenly spaced by computing a forward difference table and interpolating using  $P_n(s)$ .
- Know the definition of the backward difference operator  $\nabla$  and be able to extend the method for computing Newton Divided Difference interpolating polynomials to cases where the known values of the function are evenly spaced by computing a backward difference table and interpolating using  $P_n(s)$ .
- Be able to extend the method for computing Newton Divided Difference interpolating polynomials to cases where the known values of the function are evenly spaced by computing a forward difference table and interpolating using  $P_n(s)$ .
- Know the definition of the Hermite osculating polynomial approximating a given function and its relationship with Lagrange interpolating polynomials.
- Be able to compute the Hermite interpolating polynomial approximating a given function and use it to approximate a function at a given point.