

Math 310
Exam 1 Review Sheet

Section 1.1 - Propositional Logic

- Understand the definition of a proposition and be able to determine whether or not a given sentence is a proposition.
- Understand the definition and truth tables of the logical operators \neg , \wedge , \vee , \oplus , \rightarrow , and \leftrightarrow
- Be able to build the truth table of any compound proposition.
- Be able to translate back and forth between English statements and symbolic logical propositions.
- Understand the various ways of expressing a conditional statement in English (e.g. necessary, sufficient, only if, whenever, ...). Also know the difference between a conditional statement and its converse, inverse, and contrapositive statement.
- Understand how to apply logical operations to binary bit strings.
- Be able to solve simple logic puzzles by interpreting them in terms of logical propositions.

Section 1.2 - Propositional Equivalences

- Understand what it means for a proposition to be a *tautology*, a *contradiction*, or a *contingency*.
- Understand what it means for two propositions to be logically equivalent and be able to prove the logical equivalence of a pair of propositions by building truth tables.
- Memorize the list of standard logical equivalences (see handout).
- Be able to prove two propositions are logically equivalent using a 2-column proof and logical equivalences.
- Be able to prove that a proposition is a tautology using a 2-column proof and logical equivalences.
- Be able to negate propositions using De Morgan's Laws and other equivalences.

Section 1.3 - Predicates and Quantifiers

- Understand the definition of a predicate involving one or more variables.
- Understand the definition of the universal quantifier, the existential quantifier, and the uniqueness quantifier.
- Be able to determine the truth value of statements involving predicates and/or quantifiers.
- Understand the definition of a *counterexample* and how to use them to show that a statement is false.
- Understand how to translate English statements into statements involving predicates and quantifiers. Be able to find multiple ways of translating the same English sentence by using different predicates and/or variable domains.
- Understand the definition of logical equivalence for statements involving predicates and quantifiers.
- Be able to negate statements involving predicates and quantifiers and be able to recognize free and bound variables.
- Understand the order of operations for statements involving quantifiers.

Section 1.4 - Nested Quantifiers

- Understand how more than one quantifier can work together to form a statement involving predicates and quantifiers.
- Be able to translate English statements into symbolic statements involving *more than one* quantifier, when appropriate.
- Be able to translate symbolic statements involving predicates and *more than one* quantifier into English.
- Be able to determine the truth value of statements involving predicates and *more than one* quantifier.
- Be able to negate statements involving predicates and *more than one* quantifier.

Section 1.5 - Rules of Inference

- Know the definition of an argument and how to use a truth table to determine whether a given argument form is valid.
- Memorize the standard rules of inference for arguments with statements involving propositions (see handout).
- Memorize the standard rules of inference for arguments with statements involving predicates and quantifiers (see handout).
- Be able to translate arguments from English into symbolic form.
- Memorize the standard logical fallacies.
- Be able to recognize from the basic form of a short argument whether it is a known valid argument form or a known fallacy.
- Be able to prove whether or not a given argument is valid by constructing a 2-column proof.
- Be able to find valid conclusions from a list of premises by applying one or more rules of inference.

Section 1.6 - Introduction to Proofs

- Understand the basic terminology for paragraph proofs (see handout)
- Understand the differences between formal and informal proofs.
- Be able to write short proofs making use of: Direct proof, Contraposition, and Proof by Contradiction.
- Given a proof, be able to determine which method was used in the proof.
- Be able to find errors in false proofs.
- Understand what vacuous and trivial proofs are and be able to recognize them, including begging the question.
- Understand the definition of odd numbers, even numbers, and rational numbers.