Math 450

Programming Assignment 4

Due: Friday, December 14th

- 1. Write programs that implements each of the following numerical methods. Your algorithm should take as input a function f(t,y), an interval [a, b], an initial condition $y(a) = \alpha$, and a step size h. For the higher order Taylor Methods, you may perform the additional differentiations externally.
 - (a) Euler's Method
 - (b) Taylor's Method of order 2.
 - (c) Taylor's Method of order 4.
 - (d) The Midpoint Method.
 - (e) Modified Euler's Method.
 - (f) Heun's Method.
 - (g) Runge-Kutta Order 4.
- 2. Given the initial value problem $y' = -ty + 4ty^{-1}$, $0 \le t \le 1$, y(0) = 1, use each of your algorithms to approximate the value of y(1) using each of the algorithms you coded above:
 - (a) For h = 0.1.
 - (b) For h = 0.01
- 3. Given that the actual solution to this differential equation is: $y(t) = \sqrt{4-3e^{-t^2}}$
 - (a) Find the absolute error of each of your estimates using h = 0.1.
 - (b) Find the absolute error of each of your estimates using h = 0.01.
 - (c) Compute the ratio of each pair absolute errors you found. Do these ratios give an indication of the rate of convergence of these numerical algorithms?