

1. Complete each exercise for the functions  $f$  and  $g$  where they are defined by

$$f(x) = 2x^3 - 7x + 5 \text{ and } g(x) = 15 - 6x - x^2.$$

- (a) Do each of the following.
- Define each of the functions  $f$  and  $g$ .
  - Define a function for the sum of  $f$  and  $g$ . Evaluate on the input  $x = c$ .
  - Define a function for the quotient of  $f$  and  $g$  where  $g$  is the divisor. Evaluate on the input  $x = c$  and simplify.
  - Define a function for the composition  $f \circ g$ . Evaluate on the input  $x = c$  and simplify.
- (b) Find the **exact value** of  $f$ ,  $g$ , the sum, the quotient, and the composition when  $x = 2\sqrt{3}$ . *Simplify all of the answers.*
- (c) Evaluate  $g(a^2)$ ,  $f(3t - 2)$ , and  $g(a + h)$ . *Simplify each.*
- (d) Graph both  $f$  and  $g$  on the same coordinate plane where  $x \in [-3, 2]$ . Use standard (normal) crossed axes, make each curve a *different* solid color, show gridlines, show a title and legend, use the function names in the legend, and make the coordinate plane as wide as the display. Also, use the **Point Probe** to *estimate* the intersection points of the graph (state the intersection points in a sentence).
- (e) Evaluate each of the following limits.
- $\lim_{x \rightarrow 0} \frac{f(x)}{g(x)}$
  - $\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$

2. The 2008 Minnesota State Income Tax Schedule for the filing status of Married filing jointly or Qualifying widow(er):

Taxable income is over	But not over	Amount of Tax	Of the amount over
\$0	\$31,860	5.35%	\$0
\$31,860	\$126,580	\$1,704.51 + 7.05%	\$31,860
\$126,580	or over	\$8,382.27 + 7.85%	\$126,580

- (a) Define the tax function using a piecewise defined function. Use 'Tax' for the function name. *Does your definition consider negative income?*
- (b) Find the amount of tax owed on taxable income of \$25,000, \$60,000, and \$175,000. Show the results in *normal notation for a dollar amount*.
- (c) Graph the tax function with an appropriate scale, label the axes, and title the graph. Use boxed axes, *show at least some negative income*, and choose an appropriate maximum income.
- (d) How many line segments are there in the graph? What does the slope of each line segment represent?
- (e) Use a matrix to create a tax table from \$0 to \$200,000 with increments of \$10,000. The first column should be the taxable income and the second column should be the tax.

3. The voltage  $V$  produced by an AC generator (with  $t$  in seconds) is

$$V = 110 \cos(120\pi t).$$

- (a) *Approximate* the voltage for  $t = 1/240$ .
- (b) Use a matrix to create a table approximating the voltage to five decimal places for the times  $t = 0, 0.001, 0.002, 0.003, \dots, 0.01$ . The first column should contain the times and the second column the corresponding voltages.
- (c) Graph the voltage function for the interval  $t \in [0, 0.2]$ . Show a title and axes labels.