

Math 450
Programming Assignment 1
Due: Tuesday October 7th

Let $f(x) = x^5 - 5x^4 + 8x^3 - 5x^2 + 11x - 7$ and let $p_0 = 0$.

When needed, you can take the interval of interest to be $[0, 1]$.

1. Write a program that carries out the *Bisection Method* on $f(x)$. You do not need to make your program take arbitrary input (i.e. you can tailor it to this specific $f(x)$). Your program should take as input the appropriate number of initial guesses, an interval $[a, b]$ and a desired error tolerance TOL . It should output a root r that is within the desired tolerance and it should output N , the number of iterations it took to get to within the error tolerance. Make it clear what procedure you are using to compute the error of your approximations.
2. Write a program that carries out *Newton's Method* on $f(x)$. You do not need to make your program take arbitrary input (i.e. you can tailor it to this specific $f(x)$). Your program should take as input the appropriate number of initial guesses, an interval $[a, b]$ and a desired error tolerance TOL . It should output a root r that is within the desired tolerance and it should output N , the number of iterations it took to get to within the error tolerance. Make it clear what procedure you are using to compute the error of your approximations.
3. Write a program that carries out *Aitken's Method* on $f(x)$. You do not need to make your program take arbitrary input (i.e. you can tailor it to this specific $f(x)$). Your program should take as input the appropriate number of initial guesses, an interval $[a, b]$ and a desired error tolerance TOL . It should output a root r that is within the desired tolerance and it should output N , the number of iterations it took to get to within the error tolerance. Make it clear what procedure you are using to compute the error of your approximations.
4. Write a program that carries out *Steffensen's Method* on $f(x)$. You do not need to make your program take arbitrary input (i.e. you can tailor it to this specific $f(x)$). Your program should take as input the appropriate number of initial guesses, an interval $[a, b]$ and a desired error tolerance TOL . It should output a root r that is within the desired tolerance and it should output N , the number of iterations it took to get to within the error tolerance. Make it clear what procedure you are using to compute the error of your approximations.
5. Write a program that carries out *Müller's Method* on $f(x)$. You do not need to make your program take arbitrary input (i.e. you can tailor it to this specific $f(x)$). Your program should take as input the appropriate number of initial guesses, an interval $[a, b]$ and a desired error tolerance TOL . It should output a root r that is within the desired tolerance and it should output N , the number of iterations it took to get to within the error tolerance. Make it clear what procedure you are using to compute your initial points p_1 and p_2 , and what procedure you are using to compute the error of your approximations.
6. Use each of the programs you wrote to find an approximation of a root of $f(x)$ as given above on the interval $[0, 1]$ (with $p_0 = 0$) to within an accuracy of 10^{-5} .
7. Based on the results of your algorithms, comment on the relative effectiveness of these methods of approximating roots. Which appears to be the fastest? Which appears to be the slowest?