

Math 311  
Presentation Problems

The following problems have been compiled to both aid you in preparing for the final exam and to serve as a list of presentation eligible problems during our last regular class meeting on Tuesday, December 8th. You are expected to give a clear and correct proof, and to be able to talk your classmates through your argument as you are presenting it on the board.

1. Prove that there **do not** exist integers  $m$  and  $n$  such that  $2m + 4n = 7$ .
2. **Prove or Disprove:** Let  $a$ ,  $b$ , and  $c$  be integers. If  $ab$  divides  $c$ , then  $a$  divides  $c$ .
3. Prove that for integers  $n > 1$  that  $n!$  is even.
4. **Prove or Disprove:** The product of any 3 consecutive integers is a multiple of 3.
5. **Prove or Disprove:** If  $A$  or  $B$  are sets satisfying  $A \cup B = A \cap B$ , then  $A \cap \overline{B} = \emptyset$ .
6. Suppose  $R = \{(x, y) \in \mathbb{R}^2 : y - x \text{ is an integer}\}$ . Prove that  $R$  is an equivalence relation.
7. Prove that if  $r^2$  is irrational, then  $r$  is also irrational.
8. Describe all real numbers such that  $\lceil x + y \rceil = \lceil x \rceil + \lceil y \rceil$

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