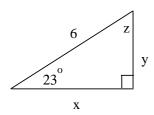
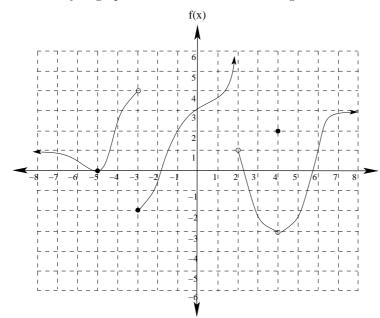
## Exam 1 - Practice Problems

- 1. Given the points A:(4,-2) and B:(-2,7):
  - (a) Find an equation for the line containing A and B
  - (b) Find the line that is perpendicular to the line you found in part (a) and containing the point (1, -1)
- 2. Find solutions to the inequality:  $\frac{x^2-1}{x^2+x-6} \le 0$ .
- 3. Given the function  $f(x) = \frac{1}{x-2}$ 
  - (a) What is the domain of f? Give your answer in interval notation.
  - (b) Find f(5) and f(2a+4)
  - (c) Find  $\frac{f(a+h)-f(a)}{h}$  (be sure to simplify your answer).
- 4. Given that  $f(x) = \frac{1}{2x-3}$  and  $g(x) = \sqrt{x^2-9}$ 
  - (a) Find  $f \circ g(2)$
  - (b) Find the domain of  $\frac{g}{f}$ ? Give your answer in interval notation.
- 5. Find the exact value of each of the following:
  - (a)  $\sin\left(\frac{7\pi}{4}\right)$
  - (b)  $\cos\left(\frac{4\pi}{3}\right)$
  - (c)  $\sin^{-1}\left(\frac{1}{\sqrt{2}}\right)$
  - (d)  $\cos^{-1}(-1)$
  - (e)  $\sin^{-1}\left(-\frac{\sqrt{3}}{2}\right)$
- 6. Find all solutions to the following equations. Give the exact answers.
  - (a)  $2\sin 3x = \sqrt{3}$
  - (b)  $\sin^2(x) \sin(x) = 0$
- 7. Find the values of x, y and z in the triangle shown below:



## 8. A function f is graphed below. Find the following:



- (a) f(-5), f(-3), and f(4)
- (b) find the domain and range of f
- (c) find the intervals where f is decreasing
- (d) find  $\lim_{x \to 4} f(x)$
- $\mathbf{x}$  (e) find  $\lim_{x\to 2^-} f(x)$  and  $\lim_{x\to 2^+} f(x)$ 
  - (f) find  $\lim_{x \to -\infty} f(x)$  and  $\lim_{x \to \infty} f(x)$
  - (g) find the points where f(x) is discontinuous, and classify each point of discontinuity.

## 9. Find the following limits:

(a) 
$$\lim_{x \to 2} \frac{3x + 7}{\sqrt{5x - 1}}$$

(b) 
$$\lim_{x \to \frac{3}{2}} \frac{2x^2 + x - 6}{4x^2 - 4x - 3}$$

(c) 
$$\lim_{x \to 2} \frac{x^4 - 16}{x^2 - x - 2}$$

(d) 
$$\lim_{x \to -2^+} \sqrt{x+2}$$

(e) 
$$\lim_{x \to 3^+} \frac{4}{\sqrt{x-3}}$$

(f) 
$$\lim_{x \to \infty} \frac{(3x-5)(2x-3)}{(2x+1)(3x-2)}$$

(g) 
$$\lim_{x \to \infty} \frac{(3x-5)(2x-3)}{(2x+1)}$$

10. Given the function

$$f(x) = \begin{cases} x^2 & \text{if } x < 1\\ 2 & \text{if } x = 1\\ 4 - x^2 & \text{if } x > 1 \end{cases}$$

- (a) Graph f(x).
- (b) Find  $\lim_{x\to 1^-} f(x)$ ,  $\lim_{x\to 1^+} f(x)$ , and  $\lim_{x\to 1} f(x)$
- (c) Is f(x) continuous at x = 1? Justify your answer.
- 11. Given that  $f(x) = x^3 + 5$ ,  $\lim_{x \to 2} f(x) = 13$ , and  $\epsilon = .01$ , find the largest  $\delta$  such that if  $0 < |x 2| < \delta$ , then  $|f(x) 13| < \epsilon$ .
- 12. Use the formal definition of a limit to prove that  $\lim_{x\to 6} 5x 21 = 9$ .
- 13. Let  $f(x) = \frac{x^2 x 2}{x^2 2x}$ .
  - (a) Find the values of x at which f is discontinuous.
  - (b) Find all vertical and horizontal asymptotes of f.
- 14. Find the x values at which  $f(x) = \frac{\sqrt{9-x^2}}{x^4-16}$  is continuous.
- 15. Use the Intermediate Value Theorem to show  $x^5 3x^4 2x^3 x + 1 = 0$  has a solution between 0 and 1.