

1. Suppose you throw a ball vertically upward. If you release the ball 7 feet above the ground at an initial speed of 48 feet per second, how high will the ball travel? (Assume gravity is $-32ft/sec^2$)
2. Use Newton's Method to approximate a real root of the function $f(x) = x^3 - 5x^2 + 27$ to 5 decimal places.
3. Use Newton's Method to approximate $\sqrt{10}$ to 5 decimal places.
4. Find each of the following indefinite integrals:

(a) $\int \frac{x^{\frac{3}{2}} - 7x^{\frac{1}{2}} + 3}{x^{\frac{1}{2}}} dx$

(b) $\int \sin^3 x \cos x dx$

(c) $\int 5x(x^2 + 1)^8 dx$

(d) $\int \frac{x}{\sqrt{x+1}} dx$

5. Solve the following differential equations under the given initial conditions:

(a) $\frac{dy}{dx} = \sin x + x^2; y = 5$ when $x = 0$

(b) $g''(x) = 4 \sin(2x) - \cos(x); g'(\frac{\pi}{2}) = 3; g(\frac{\pi}{2}) = 6$

6. Express the following in summation notation:

(a) $2 + 5 + 10 + 17 + 26 + 37$

(b) $x^2 + \frac{x^3}{4} + \frac{x^4}{9} + \dots + \frac{x^{11}}{100}$

7. Evaluate the following sums:

(a) $\sum_{k=2}^5 k^2(k+1)$

(b) $\sum_{k=3}^{20} k^3 - k^2$

8. Express the following sums in terms of n :

(a) $\sum_{k=1}^n 3k^2 - 2k + 10$

(b) $\sum_{k=3}^n k(k^2 - 1)$

9. Consider $f(x) = 3x^2 - 5$ in the interval $[3, 7]$

- (a) Find a summation formula that gives an estimate the definite integral of f on $[3, 7]$ using n equal width rectangles and using midpoints to give the height of each rectangle. You do not have to evaluate the sum or find the exact area.
- (b) Find the norm of the partition $P : 3 < 3.5 < 5 < 6 < 6.25 < 7$
- (c) Find the approximation of the definite integral of f on $[3, 7]$ using the Riemann sum for the partition P given in part (b).

10. Assume f is continuous on $[-5, 3]$, $\int_{-5}^{-1} f(x) dx = -7$, $\int_{-1}^3 f(x) dx = 4$, and $\int_1^3 f(x) dx = 2$. Find:

(a) $\int_3^{-1} f(x) dx$

(b) $\int_{-5}^1 f(x) dx$

(c) $\int_{-5}^3 f(x) dx$

(d) $\int_{-1}^{-1} f(x) dx$

(e) Find the average value of f on $[-5, -1]$

11. Evaluate the following:

(a) $\int_1^4 x^3 + \frac{1}{\sqrt{x}} + 2 dx$

(b) $\int_0^1 x^2(2x^3 + 1)^2 dx$

(c) $\int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \sin^3(2x) \cos(2x) dx$

(d) $\int_{-\pi}^{\pi} \sin x dx$

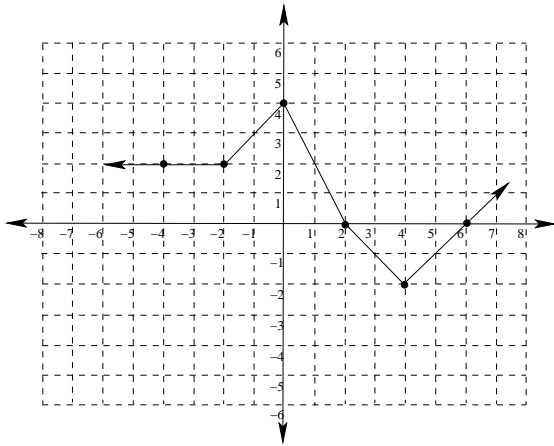
(e) $\frac{d}{dx} \left(\int_1^3 t\sqrt{t^2 - 1} dt \right)$

(f) $\int_1^3 \frac{d}{dx} \left(t\sqrt{t^2 - 1} \right) dt$

12. Suppose $G(x) = \int_2^x \frac{1}{t^2 + 1} dt$

- (a) Find $G'(2)$
- (b) Find $G'(x^2)$
- (c) Find $G''(3)$

13. Given the following graph of $f(x)$ and the fact that $G(x) = \int_{-2}^x f(t) dt$:



- (a) Find $G(6)$
- (b) Find $G'(6)$
- (c) Find $G''(6)$
14. (a) Use the Trapezoidal Rule with $n = 4$ to approximate $\int_0^4 2x^3 dx$
- (b) Find the maximum possible error in your approximation from part (a).
- (c) Use the Fundamental Theorem of Calculus to find $\int_0^4 2x^3 dx$ exactly. How far off was your estimate? How does the actual error compare to the maximum possible error?
- (d) Determine the minimum number of rectangles should be used in order to guarantee an approximation of $\int_0^4 (2x^3) dx$ is accurate to within .0005 when using the Trapezoid Rule.