

1. Evaluate each of the following integrals.

$$(a) \int (3x^2 + 2x + 1) dx$$

$$(b) \int \left(\frac{3}{t^3} + 2t + 1 \right) dt$$

$$(c) \int 5 \sin z dz$$

$$(d) \int \frac{x^2 - 2x + 5}{\sqrt{x}} dx$$

$$(e) \int (2x + 3)^2 dx$$

$$(f) \int \frac{1}{\sin^2 y} dy$$

$$(g) \frac{d}{dx} \int (x^2 + 4)^5 dx$$

$$(h) \int \frac{d}{dx} (\tan(x^2 + 7)) dx$$

2. (a) If k is a constant then $\int k^3 dx =$

(b) $\int k^3 dk =$

3. Solve the differential equation subject to the given conditions.

(a) $f'(x) = x^2 + x; f(0) = 4$

(b) $\frac{dy}{dx} = \frac{1}{\sqrt{3x+1}}; y = 2$ when $x = 1$

(c) $g''(\alpha) = 3 \cos \alpha - 2 \sin \alpha; g'(\frac{\pi}{2}) = 5; g(\frac{\pi}{3}) = 4$

6. Evaluate each of the following integrals.

$$(a) \int (3x - 2)^7 dx$$

$$(b) \int 6x^2(2x^3 + 3)^5 dx$$

$$(c) \int 3t\sqrt{4 - 3t^2} dt$$

$$(d) \int 5 \sin^3 z \cos z dz$$

$$(e) \int \frac{6x}{(x^2 + 1)^4} dx$$

$$(f) \int 2w^2 \cos(4w^3) dw$$