Math 487 Chpater 1 Quiz Review Sheet

Section 1.1 - Axiomatic Systems

• Understand the definition of an axiomatic system and its 4 components: undefined terms, defined terms, axioms, and theorems.

• Know what a model for an axiomatic system is and be able to determine whether or not a model satisfies the axioms of a given axiomatic system.

• Understand what it means for an axiomatic system to be consistent and why this is an essential property for an axiomatic system.

• Understand what it means for an axiomatic system to be complete and be able to use models to show that a given axiomatic system is not complete.

• Understand what it means for an axiomatic system to be independent and be able to determine whether or not a given axiomatic system is independent.

• Given two models, be able to determine whether or not the models are isomorphic.

• Understand the principle of duality and be able to find the dual of a given axiom.

• Given an axiomatic system, be able to prove theorems about the axiomatic system and be able to find one or more models for the given system.

Section 1.2 - A Finite Geometry

- Given the Axioms for Fano's Geometry, be able to prove theorems about this geometry.
- Memorize the standard model for Fano's geometry and know how many points and lines are in this geometry.

Section 1.3 - A Finite Projective Plane Geometry

• Given the axioms of a projective geometry, be able to determine whether or not a given model satisfies these axioms.

• Be able to show that Fano's Geometry is a projective geometry of order n = 2 and know that there are projective geometries of order p^m for any prime number p and positive integer m.

• Understand the definition of a *concurrent*.

• Know that finite projective geometries satisfy the principle of duality, and be able to prove the dual of any of the axioms for a projective geometry.

• Be able prove basic theorems about projective geometries.

• Know that a projective plane of order n has exactly $n^2 + n + 1$ points and exactly $n^2 + n + 1$ lines.