

1. Complete each exercise for the functions f and g where they are defined by

$$f(x) = 3x^2 + 4x - 4 \text{ and } g(x) = 14 - 3x - 5x^2.$$

- (a) Do each of the following.
- Define each of the functions f and g .
 - Define a function for the sum of f and g . Evaluate.
 - Define a function for the quotient of f and g where g is the divisor. Evaluate and simplify.
 - Define a function for the composition $f \circ g$. Evaluate and simplify.
- (b) Find the **exact value** of f , g , the sum, the quotient, and the composition when $x = 3\sqrt{2}$. *Simplify all of the answers.*
- (c) Evaluate $f(x^2)$, $g(2t + 3)$, and $f(a + h)$. *Simplify each.*
- (d) Graph both f and g on the same coordinate plane where $x \in [-3, 2]$. Use standard (normal) crossed axes, make each curve a *different* solid color, show gridlines, show a title and legend, use the function names in the legend, and make the coordinate plane as wide as the display. Also, use the **Point Probe** to *estimate* the intersection points of the graph (state the intersection points in a sentence).
- (e) Evaluate each of the following limits.
- $\lim_{x \rightarrow 0} \frac{f(x)}{g(x)}$
 - $\lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}$

2. The 2008 Minnesota State Income Tax Schedule for the filing status of Married filing jointly or Qualifying widow(er):

Taxable income is over	But not over	Amount of Tax	Of the amount over
\$0	\$31,860	5.35%	\$0
\$31,860	\$126,580	\$1,704.51 + 7.05%	\$31,860
\$126,580	or over	\$8,382.27 + 7.85%	\$126,580

- (a) Define the tax function in terms of a piecewise defined function. Use 'Tax' for the function name.
Did you consider negative income?
- (b) Find the amount of tax owed on taxable income of \$15,000, \$50,000, and \$150,000. Show the results in *normal notation for a dollar amount*.
- (c) Graph the tax function with an appropriate scale, label the axes, and title the graph. Use boxed axes, *show at least some negative income*, and choose an appropriate maximum income.
- (d) How many line segments are there in the graph? What does the slope of each line segment represent?
- (e) Use a matrix to create a tax table from \$10,000 to \$150,000 with increments of \$10,000. The first column should be the taxable income and the second column should be the tax.

3. The voltage V produced by an AC generator is

$$V = 220 \sin(120\pi t).$$

- (a) *Approximate* the voltage for $t = 1/240$.
- (b) Use a matrix to create a table approximating the voltage to five decimal places for the times $t = 0.001, 0.002, 0.003, \dots, 0.01$. The first column should contain the times and the second column the corresponding voltages.
- (c) Graph the voltage function for the interval $t \in [0, 0.25]$. Show a title and axes labels.