Math 262 Exam 1 Review Sheet

Calculus I Review

• Understand and be able to compute two-sided limits, one-sided limits, and limits involving infinity.

• Memorize the derivatives of functions including trigonometric functions and be able to apply differentiation rules including the product, quotient and chain rules.

- Understand how to use the first and second derivative of a function to explore the shape of the graph of a given function.
- Understand implicit differentiation and be able to find the equation of a tangent line to both implicit and explicit functions.

• Know the statements of the Intermediate Value Theorem, the Mean Value Theorem, the Extreme Value Theorem and both parts of the Fundamental Theorem of Calculus.

• Be able to evaluate both definite and indefinite integrals both my reversing standard derivative formulas and by carrying out a change of variables (substitution).

• Be able to find the Area between a function and the x-axis using the Fundamental Theorem of Calculus.

• Be able to find the area of a region enclosed between two functions by setting up definite integrals and applying the Fundamental Theorem of Calculus.

Solids of Revolution: Disks, Washers and Cylindrical Shells

• Be able to find the volume of a solid formed by revolving a planar region about either a vertical or horizontal line by setting up and evaluating a definite integral consisting of circular cross sections.

• Be able to find the volume of a solid formed by revolving a planar region about either a vertical or horizontal line by setting up and evaluating a definite integral consisting of cross sections in the shape of "washers".

• Be able to find the volume of a solid formed by revolving a planar region about either a vertical or horizontal line by setting up and evaluating a definite integral consisting of cross sections in the shape of "cylindrical shells".

Volume by Cross Sections

• Be able to find the volume of a solid described by placing cross sections over a planar region each of conform to a given shape (such as a square, rectangle, semicircle, triangle, etc.) by setting up and evaluating a definite integral.

• Be able to find the volume of a solid by interpreting it as a solid over a planar region with cross sections whose area can be computed via a function of one of the coordinate variables by setting up and evaluating a definite integral.

Arc Length and Surface Area

• Be able to find (or estimate) the arc length of a function on a given interval by setting up and evaluating a definite integral.

• Be able to find (or estimate) the surface area of a surface formed by rotating function on a given interval about either a vertical or horizontal line by setting up and evaluating a definite integral.

Work, Mass, Moments, and Center of Mass

• Understand the basic definition of Work as: $Work = (Force) \cdot (distance)$.

- Be able to find the amount of work needed to perform a given task by setting up and evaluating a definite integral.
- Understand how to find the mass of lamina with given density function by setting up and evaluating a definite integral.
- Understand how to find the Moment and center of mass of a system of point masses along the x-axis.
- Understand how to find the Moments and center of mass of a system of point masses on the xy-plane.

• Understand how to find the Moment and center of mass of a planar lamina of constant density by setting up and evaluating definite integrals.