

1. Find Taylor's Formula with remainder for the given  $f(x)$ ,  $a$ , and  $n$ .

(a)  $f(x) = \cos x$ ,  $a = \frac{\pi}{4}$ ,  $n = 4$

(b)  $f(x) = \frac{1}{(x-3)^2}$ ,  $a = 4$ ,  $n = 5$

(c)  $f(x) = e^{-x^2}$ ,  $a = 0$ ,  $n = 3$

2. If we used Problem 1a to approximate  $\cos 47^\circ$ , what decimal place accuracy could we achieve?

3. (a) Use Problem 1b to approximate  $\frac{1}{(.9)^2}$

(b) Use the Taylor remainder in Problem 1b to estimate the error in this approximation.

4. Determine the number of decimal places of accuracy that the given approximation formula yields for  $|x| \leq 0.1$ .

(a)  $e^x \approx 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4$

(b)  $\sin x \approx x - \frac{1}{6}x^3 + \frac{1}{120}x^5$

(c)  $\ln(1+x) \approx x - \frac{1}{2}x^2 + \frac{1}{3}x^3 - \frac{1}{4}x^4$