

1. Find the first four terms of the binomial series for the following functions.

(a) $(1 + x)^{-1/2}$

(b) $(1 - x^2)^{1/3}$

2. Find the binomial series for $(1 - 2x^6)^5$

3. Use an infinite series to approximate the following definite integrals to four significant digits.

(a) $\int_0^1 e^{-x^2} dx$

(b) $\int_0^{0.2} \frac{x^3}{1+x^5} dx$

(c) $\int_0^1 \frac{\sin x}{x} dx$

4. Use series representations to compute the following limits.

(a) $\lim_{x \rightarrow 3} \frac{5x^2 - 13x - 6}{\ln(x-2)}$

(b) $\lim_{x \rightarrow 0} \frac{e^x - \cos x}{\frac{1}{1-2x} - \frac{1}{1+2x}}$