

1. Find the derivative of each of the following functions.

(a) $f(x) = \ln \left| 3x^2 - 2 \right|$

(c) $f(x) = \frac{x}{\ln(x)}$

(b) $f(x) = \sqrt{\ln(\sqrt{x^2 + 2})}$

(d) $f(x) = x \ln(x) - x$

(e) $f(x) = \ln \left| \sec(x) + \tan(x) \right|$

2. Use logarithmic differentiation to find y' for

(a) $y = \ln \left(\frac{(3x - 2)^3(x + 1)}{\sqrt{1 - x^2}} \right)$

(b) $y = \frac{\sqrt{x^2 - 36}(x^2 - x - 6)}{x^2 + 7x + 12}$

3. Show that $f(x) = (x - 2)^2 + 5$ is not one-to-one.

4. (a) Prove that $g(x) = \frac{3x - 2}{x + 3}$ is one-to-one.

(b) Find the inverse function for g .

5. Compute the following integrals.

$$(a) \int_{-3}^5 \frac{1}{5x+63} dx$$

$$(d) \int (1 + \sec(x))^2 dx$$

$$(b) \int \frac{5x}{x^2+4} dx$$

$$(e) \int_1^{e^2} \frac{(5 + 6 \ln(x))^5}{x} dx$$

$$(c) \int \frac{\ln(x)}{x} dx$$

$$(f) \int \tan(x) + \sin(x) dx$$

6. (From the 200? AP Calculus AB exam) Let f be the function defined by $f(x) = k\sqrt{x} - \ln(x)$ for $x > 0$, where k is a positive constant.

(a) Find $f'(x)$ and $f''(x)$.

(b) For what value of the constant k does f have a critical point at $x = 1$? For this value of k , determine whether f has a relative minimum, relative maximum, or neither at $x = 1$.

(c) For a certain value of the constant k , the graph of f has a point of inflection on the x -axis. Find this value of k .