



7. Let  $f$  be the transformation given by the matrix  $A = \begin{bmatrix} 1 & 0 & 2 \\ 0 & 1 & 3 \\ 0 & 0 & 1 \end{bmatrix}$

- Find the image of the points  $P(1, 3, 1)$  and  $Q(-2, 5, 1)$  under this transformation.
- Find the image of the line  $[1 - 24]$  under this transformation.
- What transformation is this?

8. Given the points  $P(2, 1, 1)$  and  $Q(4, 2, 1)$

- Find the matrix of a *translation* that maps  $P$  to  $Q$ .
- Find the matrix of a *reflection* that maps  $P$  to  $Q$ .
- Find the matrix of a *rotation* that maps  $P$  to  $Q$ .

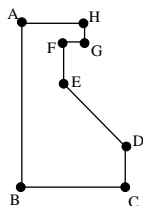
9. Consider the following transformation matrices:

$$A = \begin{bmatrix} 1 & 2 & 1 \\ 3 & 0 & -1 \\ 2 & 1 & 0 \end{bmatrix} \quad B = \begin{bmatrix} 1 & -1 & 3 \\ 2 & 1 & -1 \\ 0 & 0 & 1 \end{bmatrix} \quad C = \begin{bmatrix} 1 & 0 & -5 \\ 0 & -1 & 3 \\ 0 & 0 & 1 \end{bmatrix}$$

$$D = \begin{bmatrix} 0 & 1 & 3 \\ 1 & 0 & -1 \\ 0 & 0 & 1 \end{bmatrix} \quad E = \begin{bmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} & 0 \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad F = \begin{bmatrix} 1 & 0 & -5 \\ 0 & 1 & -3 \\ 0 & 0 & 1 \end{bmatrix}$$

- Which of these are the the matrix of an affine transformation of  $\mathbb{E}$ ?
- Which of these are the the matrix of an isometry of  $\mathbb{E}$ ?
- Which of these are the the matrix of an direct isometry of  $\mathbb{E}$ ?
- Which of these are the the matrix of a rotation of  $\mathbb{E}$ ?
- Which of these are the the matrix of a translation of  $\mathbb{E}$ ?

10. Given the plane figure in  $\mathbb{E}$  shown below, accurately draw the image of this figure under each of the following isometries:



- $R_{B,90}$
- $T_{FG}$
- $R_\ell$ , where  $\ell = \overleftrightarrow{HG}$ .
- $R_\ell$ , where  $\ell = \overleftrightarrow{ED}$ .
- $G_{CD}$

11. Prove or Disprove:

- The set of all *translations* of  $\mathbb{E}$  forms a group under composition.
- The set of all *rotations* of  $\mathbb{E}$  forms a group under composition.
- The set of all *indirect isometries* of  $\mathbb{E}$  forms a group under composition.

12. Let  $\square ABCD$  be the unit square centered at the origin in  $\mathbb{E}$ .

- Give a complete list of all of the symmetries of  $\square ABCD$ .
- Show that the set of isometries that you found in part (a) forms a group under composition.