

*Show all work for credit. Also, give exact answers unless otherwise noted.*

1. Assume that each equation determines a differentiable function  $f$  such that  $y=f(x)$ , find  $f'(x)$ .

(a)  $y^2 + x^2 = 2x + 3y^2$

(b)  $2xy = x^2 - \sqrt{y}$

2. Assume that each equation determines a differentiable function  $f$  such that  $y = f(x)$ , find  $f'(x)$ .

(a)  $x \sin y + y \sin x = 1$

(b)  $x^2(x-y)^2 = x^2 - y^2$

3. Find an equation of the tangent line to the graph of  $(x^2 + y^2)^2 = 50xy$  at the point  $(2, 4)$ .

4. Assume  $t^2v^3 = 1$  determines a function  $v = f(t)$ , use implicit differentiation to show that  $v'' = \frac{10}{9}v^4$ .

5. Assume that a rectangle has side lengths  $a$  and  $b$ .

a. Find a formula for the area  $A$  of the rectangle in terms of  $a$  and  $b$ .

b. Assume that  $a$  and  $b$  are changing over a period of time, and that  $a(t) = t^2 + t$  and  $b(t) = t^3 - t$  after  $t$  seconds. Find a function  $A(t)$  that gives the area of the rectangle at time  $t$ .

c. Use the formula from part b to find  $\frac{dA}{dt}$ .

d. Now, use implicit differentiation on your formula from part a to find  $\frac{dA}{dt}$ . Compare your answer with what you found in part c.