- 1. For each quadratic function given below, find the coordinates of the vertex, and find the equation for the line of symmetry for the graph of the function.
 - (a) $f(x) = (x-5)^2 + 12$ (b) $f(x) = (x+3)^2 - 8$
 - (c) $f(x) = 2x^2 12x + 22$
 - (d) $f(x) = -4x^2 + 16x 13$
- 2. For each quadratic function given below, find the vertex, line of symmetry, and (if applicable) the *x*-intercepts of the function. Then graph the function carefully in the *xy*-plane.

(a)
$$f(x) = x^2 - 4x$$

(b)
$$f(x) = 6x^2 + 7x - 24$$

- (c) $f(x) = -2x^2 + 20x 43$
- 3. For each polynomial function given below, use the degree of the polynomial and the sign of the leading coefficient to describe the end behavior of the polynomial.

(a)
$$f(x) = 5x^4 - 3x^2 + 7$$

(b)
$$f(x) = -2x^3 + 4x^2 - 15x + 12$$

- (c) $f(x) = 12x^5 5x^4 + 3x^2 12x + 7$
- (d) $f(x) = -7x^6 + 5x^4 13x^3 + 21x^2 + 15x + 23$

4. For each polynomial function given below, find the zeros of the polynomial and also give the multiplicity of each zero.

(a) $f(x) = x^4 + 3x^3 - 4x^2$ (b) $f(x) = x^3 + 2x^2 - 4x - 8$ (c) $f(x) = x(x-4)^4(x+3)^3$

(d)
$$f(x) = x^3(x-2)^2(x^2-4)^5$$

5. Use the intermediate value theorem to show that $f(x) = 2x^3 + 5x^2 - 3$ has a zero between x = -3 and x = -2

- 6. For each of the following quadratic functions:
 - Find the vertex and axis of symmetry
 - Find all intercepts
 - Graph the function and list its range in interval notation
 - (a) $f(x) = 4(x+3)^2 7$
 - (b) $f(x) = -3(x-4)^2 + 11$
 - (c) $f(x) = x^2 2x 15$

(d)
$$f(x) = 3x^2 - 2x - 4$$

- (e) $f(x) = -2x^2 + 8x 1$
- 7. Among all pairs of numbers whose sum is 20, find the pair whose product is as large as possible. Also find the value of the maximum product.
- 8. Suppose that you have 600 feet of fencing to enclose a rectangular field that borders a river on one side. If you do not fence the side along the river, find the length and width of the maximum sized field that you can fence in.
- 9. Find the zeros for each polynomial function given. Also find the multiplicity of each zero.

(a)
$$f(x) = x^3 - x^2 - 9x + 9$$

(b) $f(x) = 2x^3 - 5x^2 - 12x$

(c)
$$f(x) = x^2(x-1)(x+3)^3$$

(d) $f(x) = x^3(x-2)(x^2-4)^2$

- 10. Use the Leading Term Test to determine the end behavior for each polynomial function given.
 - (a) $f(x) = x^5 4x^3 + 17x^2 + 5x 14$ (b) $f(x) = -3x^8 - 5x^5 + 3x^2 + 17$ (c) $f(x) = x^2(2x - 1)(x + 2)$
 - (d) $f(x) = -4x^2(x-2)(x^2+1)$
- 11. Use the Intermediate Value Theorem to show that each polynomial has a zero on the given interval.
 - (a) $f(x) = x^4 3x^2 + 5x 7$ on [1, 2] (b) $f(x) = 4x^3 - 12x^2 + 25x - 100$ on [3, 5]
- 12. Use the Leading Coefficient test to determine the end behavior, find all x-intercepts and their multiplicities, find the y-intercept and any symmetry, and then graph the given polynomial.
 - (a) $f(x) = 2x^3 + 3x^2 2x$ (b) $f(x) = x^3 - x^2 - 16x + 16$ (c) $f(x) = x^2(x-1)(x+4)$ (d) $f(x) = x^3(x+1)(x-2)^2(x-4)$
- 13. Use Long Division to find the following Quotients:

(a)
$$\frac{4x^4 - 4x^2 + 6x}{x - 4}$$

(b)
$$\frac{x^4 - 3x^2 + 7x + 5}{x^2 + 1}$$

(c)
$$\frac{3x^5 - 7x^3 + 5x^2 - 3}{x^2 - x + 3}$$

14. Use synthetic division to find the indicated function values:

(a) f(7) if $f(x) = x^3 - 4x^2 + 7x - 5$ (b) f(-1) if $f(x) = x^5 - 3x^3 + 3x + 4$ (c) f(2) if $f(x) = x^7 - 3x^3 + 4x - 1$

15. Solve the following equations:

- (a) $2x^3 3x^2 11x + 6 = 0$ given that -2 is a zero of $f(x) = 2x^3 3x^2 11x + 6$
- (b) $3x^3 + 7x^2 22x 8 = 0$ given that $-\frac{1}{3}$ is a zero of $f(x) = 3x^3 + 7x^2 22x 8$
- 16. Use the Rational Zero Theorem to find all possible zeros for each polynomial given.

(a)
$$f(x) = x^3 + 3x^2 - 6x - 8$$

(b) $f(x) = 2x^4 + 3x^3 - 11x^2 - 9x + 15$

(c) $f(x) = 4x^5 - 8x^4 - x + 2$

17. Find a 5th degree polynomial f(x) for which $\frac{1}{2}$, -1, 2, and $\pm i$ are all zeros and with f(1) = 12.

18. Solve the following inequalities. Express your solution in interval notation and graph the solution on a number line.

(a)
$$2x^2 + x - 6 > 0$$

(b) $3x^2 + 5x + 4 \le 2x^2 + 3x + 7$
(c) $\frac{x^2 + 2x + 1}{x - 3} \ge 0$
(d) $\frac{(x + 3)^2(x - 2)}{(x + 4)(x + 2)} \le 0$
(e) $\frac{1}{x - 2} \ge \frac{3}{x + 1}$