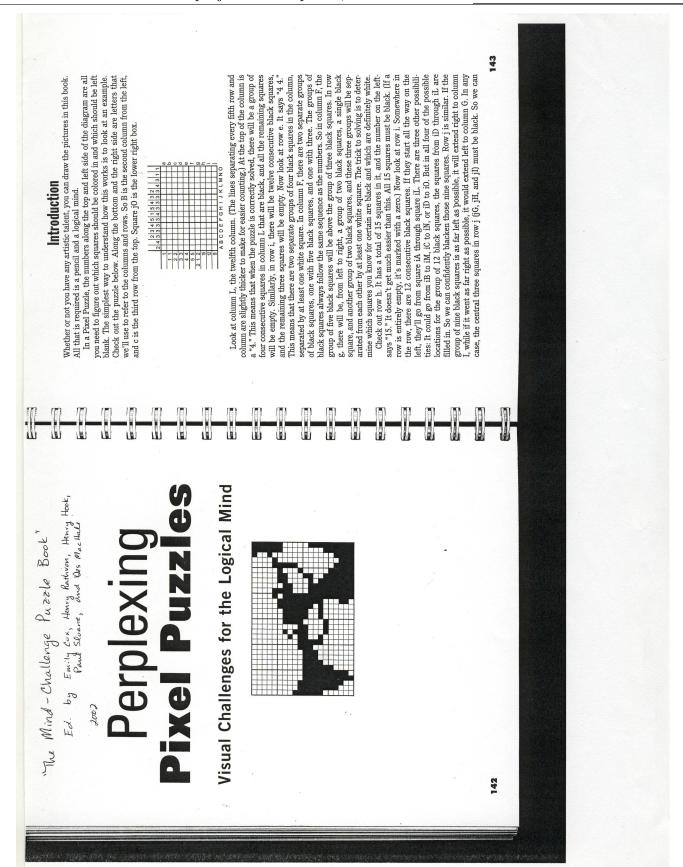
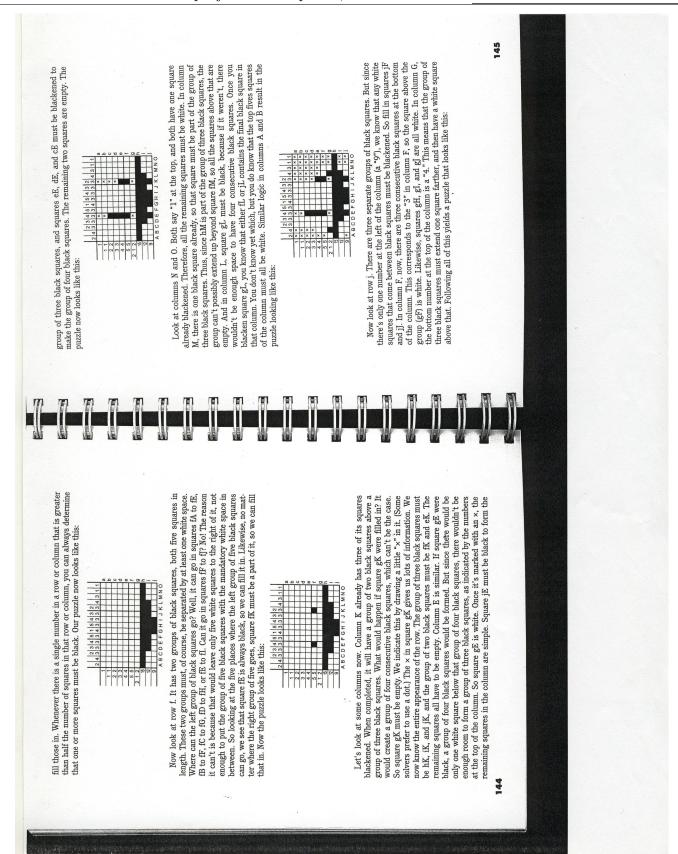
There is a pencil-puzzle known by several different names, some of which that I've come across are "Paint-doku", "Pencil Pixel Puzzles", "Picture Puzzles", "O'Ekaki", and "Nonograms". Since the first term that I came across for this kind of puzzle is O'Ekaki, that is the term that I am going to use. The puzzle, and some basic strategy, are described in the following pages. In the following, I am going to make a distinction between an O'Ekaki puzzle and an O'Ekaki solution. A puzzle is one where the grid is still blank. The dimensions have been determined, as have the numbers that are the clues at the top of each column and start of each row. A solution is a filled in grid that is consistent with the clues. (Note that in O'Ekaki the puzzles published are in general recognizable pictures, hence some of the names, the puzzles do not have to be restricted to those that make pictures. A lot of them look more like ink-blots either way.)

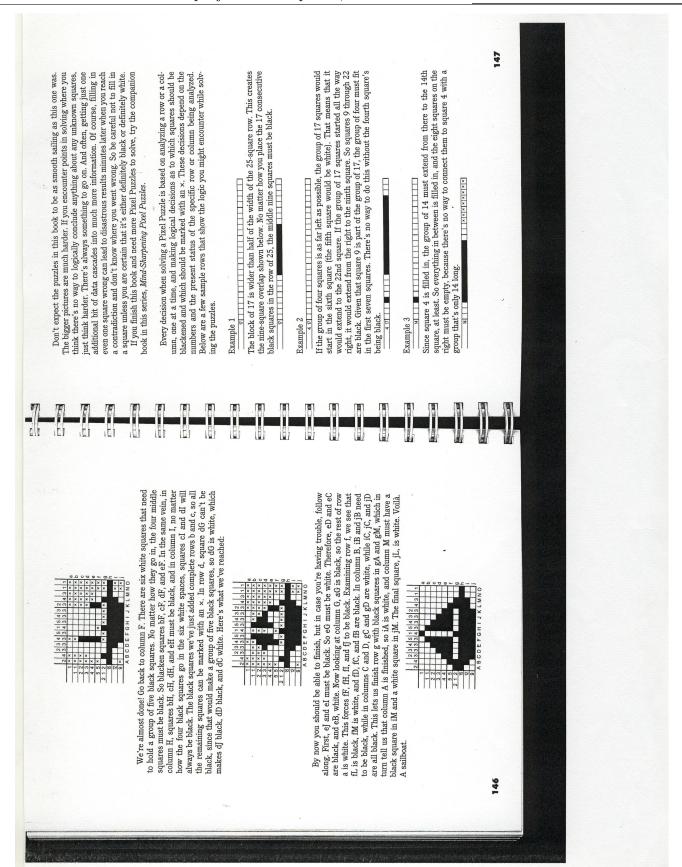
- (a) Consider a 2×2 O'Ekaki grid. Note that there are 16 possible solutions. Prove or disprove the following conjecture: There are 16 puzzles, each of which has a unique solution.
- (b) Form a conjecture for the number of possible O'Ekaki solutions for a general grid of size  $m \times n$ . Prove your conjecture.
- (c) Find a counterexample to the following conjecture: Every  $5 \times 5$  O'Ekaki puzzle has a unique solution.



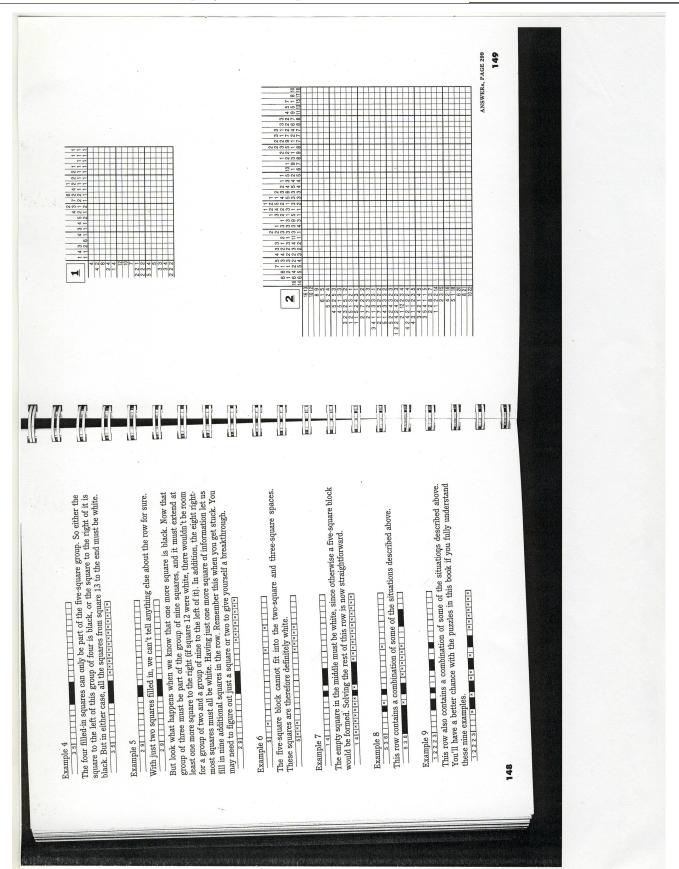
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