

This miniproject asks you to investigate certain graphs.
Do the following problems.

- (a) Draw a simple graph with five vertices and six edges.
- (b) Draw a simple graph with six vertices and ten edges.
- (c) Draw a simple graph with four vertices and three edges.
- (d) Each of the graphs that you drew in the previous three parts have at least two vertices with the same degree. Find such a pair of vertices in each of your three graphs. State both the vertices and their degree.
- (e) Prove: In a simple graph with at least two vertices, there exist at least two vertices with the same degree.