Spring 2011 Math 310 Miniproject for Chapter 10, Section 4b Name:

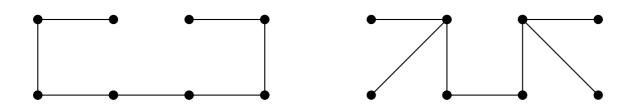
This project asks you to work with different spanning trees of the same graph.

The distance between two spanning trees  $T_1$  and  $T_2$  of a simple connected graph is the number of edges that are in  $T_1$  or  $T_2$  that are not common to  $T_1$  and  $T_2$ . (So dist  $(T_1, T_2) = |(T_1 \cup T_2) - (T_1 \cap T_2)|$ .)

(a) Find the distance between the two spanning trees below of the complete graph  $K_6$ .



- (b) Given a pair of spanning trees  $T_1$  and  $T_2$ , it is possible to find a sequence of spanning trees from  $T_1$  to  $T_2$  such that each tree can be formed from the previous one by removing just one edge and replacing it with another. Find such a sequence between the two trees given above. (Note that I am not asking you to actually prove the fact given.)
- (c) Find the distance between the two spanning trees below.



(d) Find a sequence, such as the one given in part (b), between the two trees in part (c).