

This miniproject asks you to investigate the concept of *dense* elements of a poset.

**Definition:** A poset  $(R, \preceq)$  is said to be ***dense*** if for all  $x \in R$  and  $y \in R$  with  $x \preceq y$ , then there is an element  $z \in R$  such that  $x \preceq z \preceq y$ .

Prove: The poset of the rational numbers with the usual  $\leq$  is a dense poset.