

## Section 3.1 - Statements, Connectives, Quantifiers Read pp. 82-88

**Statement:** in logic a statement is a declarative sentence that is either true or false. We represent statements by lower case letters such as  $p$ ,  $q$ , or  $r$ .

Examples of things that are **NOT statements**: Questions, commands, exclamations, and paradoxes are not statements because they do not have the quality of being “true” or “false”.

**Paradox:** a sentence that cannot be assigned a truth value because it contradicts itself. Example: “This statement is false.”

**Truth value:** The quality of being “true” or “false” is the statement’s truth value.

Which of the following are **statements** in the mathematical sense?

	Statement (in mathematics)	Truth Value
This year February has 29 days.		
$3 \times 2 = 4 + 2$		
$\{1, 2, 3\} = \{4, 5, 6\}$		
Do you have a car?		
All rules have exceptions		

### Types of Statements:

- **Simple Statement:** a statement that contains a single idea. Example: It is a sunny day.
- **Compound Statement:** a compound statement contains several ideas combined together. The words used to join the ideas of a compound statement together are called **connectives**.

### 5 Logical Connectives:

- **And** (“but” is sometimes used in place of “and”) as in “I am going, but Mary is not.”
- **Or**
- **Not**
- **If , then** Regardless of order in everyday language, “IF” introduces the hypothesis and “THEN” introduces the conclusion. In symbols, the hypothesis “IF”, ALWAYS goes first.  
Example: If it rains, I will not go. I will not go if it rains. Both are written the same way in symbols.
- **If and Only If**

## Memorize these:

### Logical Connectives and their Special Mathematical Names and Symbols

word or phrase	Special Math Name	Symbol
and (both, the overlap)	conjunction	$\wedge$ (like intersection in sets)
or (one or the other, or both)	disjunction,	$\vee$ (like union in sets)
if . . . then (implies)	conditional	$\rightarrow$
If and only if (iff)	biconditional	$\leftrightarrow$
not	negation	$\sim$

In symbolic logic, we let letters stand for statements, the way we let letters stand for numbers in algebra.

Translating the compound sentence: Today is Friday and I have a test.

Let P = Today is Friday  
Q = I have a test.

In symbols:

**Quiz Yourself #4-5 (p. 86, 87 of text)** Write each statement in symbolic form:

**d: I will buy a DVD player.**

**i: I will buy an iPod.**

(a) I will not buy a DVD player or I will not buy an iPod. \_\_\_\_\_

(b) I will not buy a DVD player and I will buy an iPod. \_\_\_\_\_

**f: I fly to Houston**

**q: I will qualify for frequent flyer miles**

(a) If I do not fly to Houston, then I will not qualify for frequent flyer miles.

\_\_\_\_\_

(b) I fly to Houston if and only if I will qualify for frequent flyer miles.

\_\_\_\_\_

**Negation applies only to the thing it is immediately next to.**

$\sim P \wedge Q$  means \_\_\_\_\_

$\sim(P \wedge Q)$  means \_\_\_\_\_

**Clues for parentheses:**

- “It is false that” or “It is not true that” (everything after the word ‘that’ is in parentheses)
- **Commas** (either the phrase before the comma or the phrase after the comma will be in parentheses – which ever one is compound.)
- “Neither A nor B” means “not” ( A or B)

**Important Counter-Intuitive Fact: (don’t let this trip you up)**

$\sim(A \wedge B) = \sim A \vee \sim B$  (and is not equal to  $\sim A \wedge \sim B$  like you might think).

Write each statement in symbolic form given that

P = Today is Monday

Q = Tomorrow is Wednesday

R = Tomorrow is Tuesday

T = Today is Tuesday

- It is false that today is Monday or tomorrow is Wednesday.
- Neither is today Monday nor is tomorrow Wednesday.
- If today is Monday, then tomorrow is Tuesday or tomorrow is Wednesday.
- Today is Tuesday if and only if tomorrow is Wednesday.
- Tomorrow is Wednesday implies that today is Monday. (we can write false statements)