

## Ch. 13 Chemical Kinetics

- "we can predict reaction products, + energetics, now we want to learn about speeds"
- some reactions faster than others!

"What controls how fast?"

- car rusts
- medicine reacts
- TNT explodes?
- milk sours
- ice cream metabolizes
- sugar in candy bar  
 $\Rightarrow \text{CO}_2 + \text{H}_2\text{O} + \text{energy}$

Factors (other than chems themselves)

- ① concentration
- ② temperature
- ③ "catalysts"

### 13.1 Reaction Rate



$\frac{\text{change in "thing"}}$   
 $\text{change (in } x\text{) per time interval}$      $\frac{\Delta x}{\Delta t}$

Ex: mph

Any average rate can be determined between measurements at 2 points in time

13-2

Rate: change in something ( $x$ ) per time interval =  $\frac{\Delta x}{\Delta t}$

Ex: What is average speed of car that between 10:00 ( $t_1$ ) and 10:30 ( $t_2$ ) travels from point O ( $x_1$ ) to 30 miles away ( $x_2$ )?

$$\frac{\Delta x}{\Delta t} = \frac{x_2 - x_1}{t_2 - t_1} = \frac{30 \text{ mi} - 0 \text{ mi}}{10:30 - 10:00} = \frac{30 \text{ mi}}{30 \text{ min}} = \boxed{\frac{1 \text{ mile}}{\text{minute}}}$$

$$\frac{1 \text{ mile}}{\text{min}} \cdot \frac{60 \text{ min}}{1 \text{ hour}} = \frac{60 \text{ miles}}{1 \text{ h}} = \boxed{60 \text{ mph}}$$

Ex  $A \rightarrow B$

Chemical rate defined by changes in concentration ( $[A]$ ) per time interval

$$\text{rate} = \frac{\Delta [B]}{\Delta t} = -\frac{\Delta [A]}{\Delta t}$$

### Notes

① rates can be written based on products or reactants, which are linked by stoichi.

$\Rightarrow [B]$  increases as  $[A]$  decreases  
(of change) (Fig 15.1)

② rate decreases with time

- declines as S.M. is depleted  
(T-11C, Table 14.2, brown)

③ Rate Can be Found from:

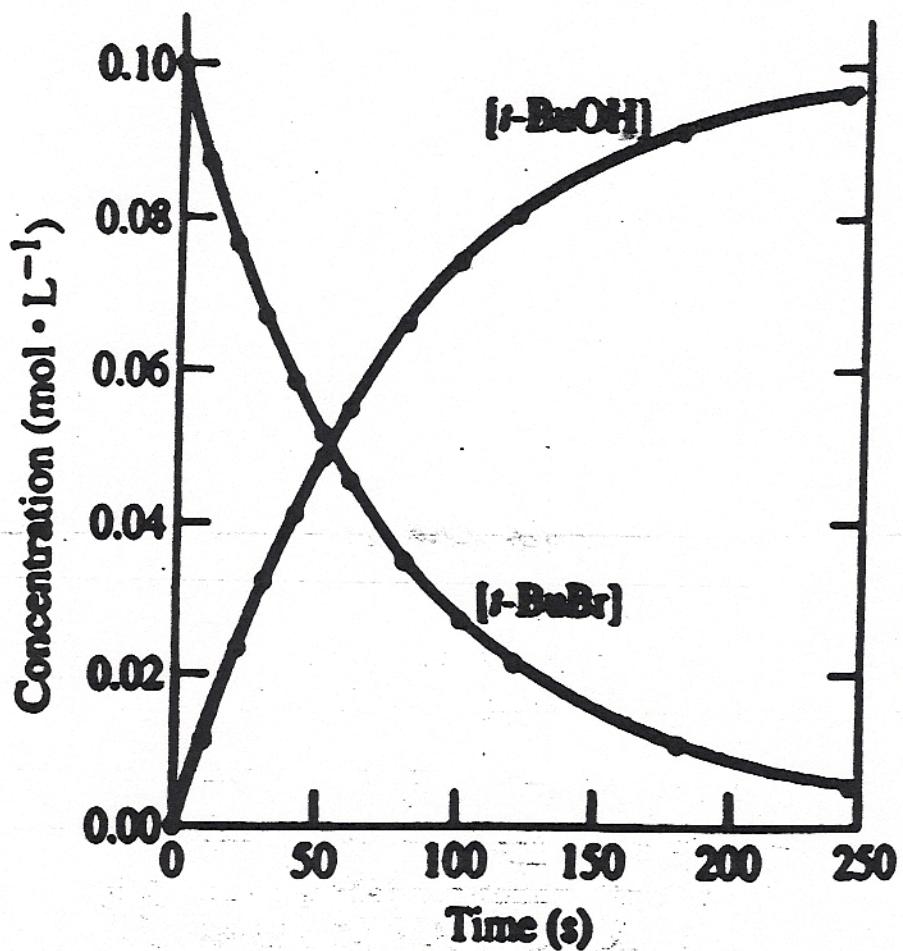
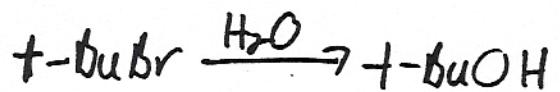
a. 2 Time Points (T-11C, Table 14.2, brown)

b. Known rate of change for another chemical  
(factor coefficients!)

c. Graphical analysis (not tested)

- tangent slope, or calculus (rate,  $= \frac{d[B]}{dt}$ )  
(T-11, Fig 15.2, brown)

④ The relative rate of change for reactants/product has stoichiometric relationships

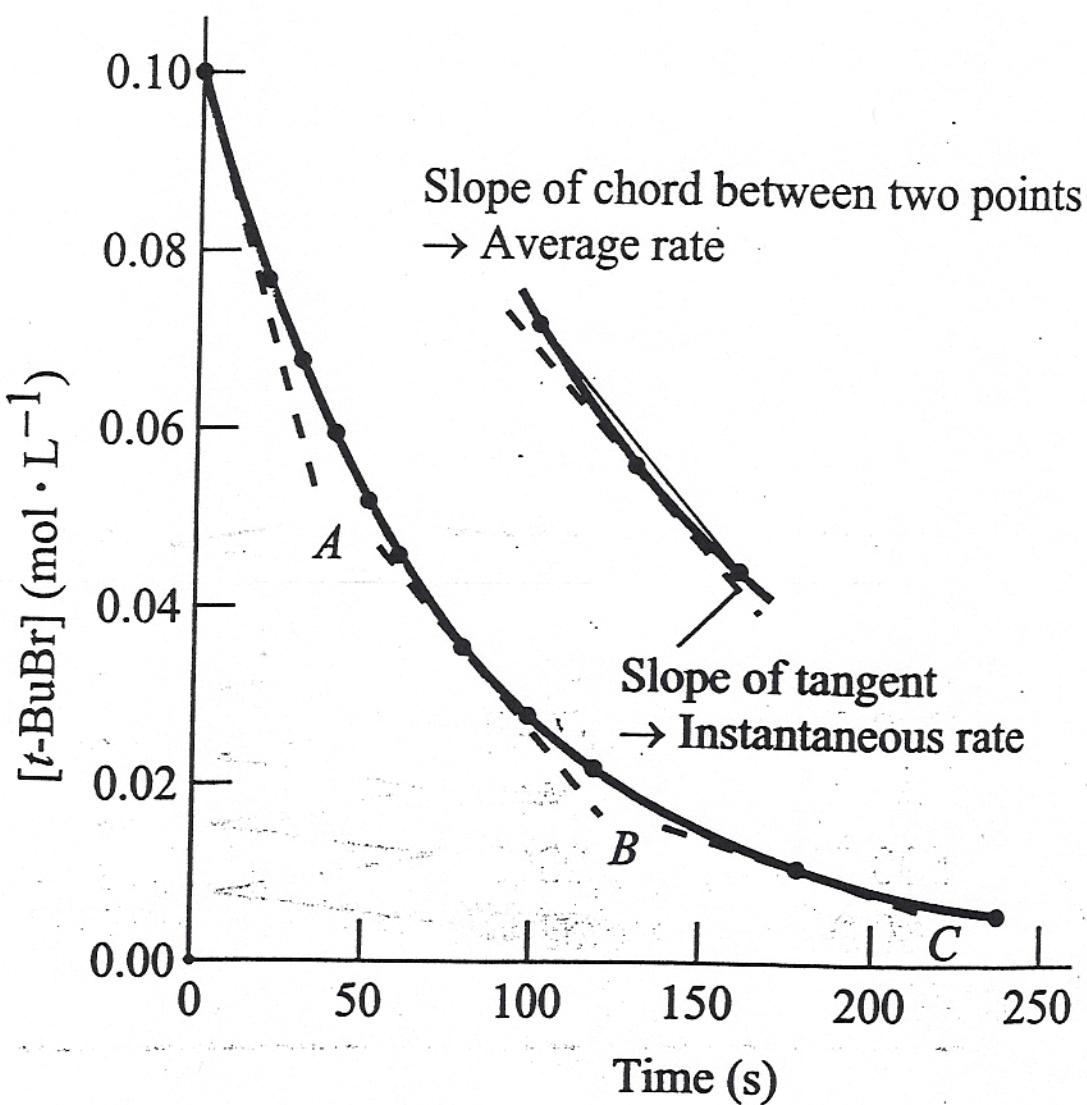


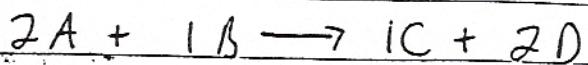
**FIGURE 15.1 Concentration Changes during the Reaction of *t*-Butyl Bromide with Hydroxide Ion** The reaction was carried out with excess water at 55°C in 20% aqueous ethanol.

TABLE 14.2 Rate Data for Reaction of  
C<sub>4</sub>H<sub>9</sub>Cl with Water

Time, <i>t</i> (s)	[C <sub>4</sub> H <sub>9</sub> Cl] (M)	Average Rate (M/s)
0.0	0.1000	
50.0	0.0905	1.9 × 10 <sup>-4</sup>
100.0	0.0820	1.7 × 10 <sup>-4</sup>
150.0	0.0741	1.6 × 10 <sup>-4</sup>
200.0	0.0671	1.4 × 10 <sup>-4</sup>
300.0	0.0549	1.22 × 10 <sup>-4</sup>
400.0	0.0448	1.01 × 10 <sup>-4</sup>
500.0	0.0368	0.80 × 10 <sup>-4</sup>
800.0	0.0200	0.560 × 10 <sup>-4</sup>
10,000	0	

T 111 Fig. 15.2 Rate of Hydrolysis of *t*-Butyl Bromide





① If the concentration of B is dropping at a rate of  $0.5\text{ M/min}$ , what is the rate of change for the following?

A:

C:

D:

② If A is dropping at  $0.8\text{ M/min}$ , what is the rate of change for:

B:

C:

D:

③ Write the rate law, relative to each, beginning with B. Put +/- signs so that rate ends up being positive.

(13-11)

### 13.3 Rate Law and Order of Reaction:

A. The "Overall Order" of a reaction is the sum of the individual orders (practice 13-7)

#### B. Calculations for 1<sup>st</sup> Order Reactions

$$r = k[A] = \frac{-\Delta [A]}{\Delta t}$$

Calculus,  
integrate

$\ln[A]_t = -kt + \ln[A]_0$   $y = mx + b$  form!

useful for graphical analysis

linear plot of  $\ln[A]_t$  vs. time gives slope =  $-k$

only 1<sup>st</sup> order straight line

or  $\ln\left(\frac{[A]_t}{[A]_0}\right) = kt$  Used for 2-point analysis

- Application:
1.  $[A]_t$  at any time  
find
  2. time for  $[A]_0 \rightarrow [A]_t$ ,
  3.  $k$

#### Handling "ln"

- ① enter  $[A]_0 / [A]_t$  ratio, then hit LN button
- ② "antiln"  $\ln \frac{100}{x} = 1.83$  find x

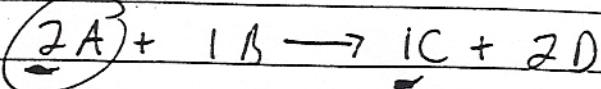
enter 1.83, hit  $e^x$

result:  $6.23 = \frac{100}{x}$   $|x =$  

$x = 100/6.23 = 16$

Chem 160-Jasperse Ch. 13 In Class Packet

(13-4)



① If the concentration of B is dropping at a rate of  $0.5 \text{ M/min}$ , what is the rate of change for the following?

A:  $\downarrow 1.0 \text{ M}$

C:  $\uparrow 0.5 \text{ M}$

D:  $\uparrow 1.0 \text{ M}$

② If A is dropping at  $0.8 \text{ M/min}$ , what is the rate of change for:

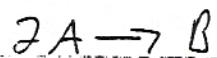
B:  $\downarrow 0.4 \text{ M}$

C:  $\uparrow 0.4 \text{ M}$

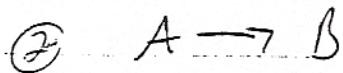
D:  $\uparrow 0.8 \text{ M}$

③ Write the rate law, relative to each, beginning with B. Put +/- signs so that rate ends up being positive.

$$\text{rate} = \frac{-\Delta(B)}{\Delta t} = \frac{-\Delta(A)}{\Delta t} = \frac{-\Delta(C)}{\Delta t} = \frac{-\Delta(D)}{\Delta t}$$



① If  $\frac{\Delta A}{\Delta t} = -0.10 \text{ M/s}$ , what is  $\frac{\Delta B}{\Delta t}$ ?



a. Calculate the average rate from  $0 \rightarrow 10 \text{ sec}$   
if  $[A]$  goes from  $0.1000 \rightarrow 0.0876 \text{ M}$ ?

b. If  $[B]=0$  at  $0 \text{ sec}$ , what is it after  
 $5 \text{ sec}$ ?  $[B]$

(13-5)

 $2A \rightarrow B$ 

① If  $\frac{\Delta A}{\Delta t} = -0.10 \text{ m/s}$ , what is  $\frac{\Delta B}{\Delta t}$ ?

$$\boxed{-0.05 \text{ m/s}}$$

②  $A \rightarrow B$

a. Calculate the average rate from  $0 \rightarrow 10 \text{ sec}$   
if  $[A]$  goes from  $0.1000 \rightarrow 0.0876 \text{ M}$ ?

$$\frac{\Delta A}{\Delta t} = \frac{0.1000 - 0.0876}{10 \text{ s} - 0 \text{ s}} = \frac{0.0124 \text{ M}}{10 \text{ sec}} = \boxed{-0.00124 \text{ M/sec}}$$

b. If  $[B]=0$  at  $0 \text{ sec}$ , what is it after  
 $5 \text{ sec}$ ?  $[B]$

$$B: \frac{0.00124 \times 5 \text{ sec}}{\text{sec}} = \boxed{0.0062 \text{ M}}$$

## 13.2 Effect of Concentrations on Rate

- since reactants must collide to react, rate depend on concentrations

## A. General "Rate Law"

$$\text{rate} = k[A]^x[B]^y[C]^z \quad A, B, C \text{ reactants or catalyst}$$

- ① describes dependence of rate on each conc.

$$\text{rate} \propto [A]^x \quad \text{rate} \propto [B]^y \quad \text{rate} \propto [C]^z$$

- ex: if  $x=0$  then doubling  $[A] \Rightarrow$  no change in rate
- $x=1 \quad \Rightarrow$  rate doubles (direct proportion)
- $x=2 \quad \Rightarrow$   $\times 4$  (proportion)

- ②  $k$  is "rate constant": rate changes with time

- conc, but  $k$  does not

- ③ each reaction has own rate law and constant

- both must be determined experimentally

- can't tell from eqn stoichiometry

13.7-1 [problem: find  $k$  given rate law, rate + conc.]

Given rate law and  $k$ , can find rate given conc  
problem 13.7-2

- ④ Examples of rate laws - wide variety, can't deduce from balanced eqn

- ⑤ "Order" = exponent for reactant  $x=1 \Rightarrow$  first  $2 \Rightarrow$  second, etc.

$$\text{rate} = k[A]^2$$

① If rate is  $3.6 \times 10^{-3} \text{ M/s}$  when  $[A] = 0.20 \text{ M}$ , what is  $k$ ?

② If  $k = 0.090 \text{ M}^{-1}\text{s}^{-1}$  and  $[A] = 0.001 \text{ M}$ , what is the rate?

Rate Law Examples	Effect on rate when [A] is doubled	"Order" of A	Overall Rxn Order	Rate Constant Units
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$$r = k[A]$$

$$r = k[A][B]$$

$$r = k[A]^2[B]$$

$$r = k[A]^3[B]$$

$$r = k[B]$$

$$r = k[A]^{1/2}[B]$$

$$\text{rate} = k[A]^2$$

① If rate is  $3.6 \times 10^{-3} \text{ M/s}$  when  $[A] = 0.20 \text{ M}$ , what is  $k$ ?

$$3.6 \times 10^{-3} \frac{\text{M}}{\text{s}} = k (0.20 \text{ M})^2$$

$$k = \frac{3.6 \times 10^{-3} \text{ M/s}}{0.040 \text{ M}^2}$$

$$k = 0.090 \text{ M}^{-1} \text{s}^{-1}$$

② If  $k = 0.090 \text{ M}^{-1} \text{s}^{-1}$  and  $[A] = 0.00 \text{ M}$ , what is the rate?

$$r = (0.090 \text{ M}^{-1} \text{s}^{-1})(0.00 \text{ M})^2 = 0.324 \text{ M} \cdot \text{s}^{-1}$$

Rate Law Examples	Effect on rate when [A] is doubled	Effect on rate when [B] is tripled	"Order" of A	Overall Order	Rate Constant	Units
$r = k[A]$	$\times 2$	$\times 10$	1 <sup>st</sup>	1 <sup>st</sup>	$\text{M}^{-1} \text{s}^{-1}$	
$r = k[A][B]$	$\times 2$	$\times 10$	1 <sup>st</sup>	2 <sup>nd</sup>	$\text{M}^{-1} \text{s}^{-1}$	
$r = k[A]^2[B]$	$\times 4 (2^2)$	$\times 100 (10^2)$	2 <sup>nd</sup>	3 <sup>rd</sup>	$\text{M}^{-2} \text{s}^{-1}$	
$r = k[A]^3[B]$	$\times 8 (3^3)$	$\times 1000 (10^3)$	3 <sup>rd</sup>	4 <sup>th</sup>	$\text{M}^{-3} \text{s}^{-1}$	
$r = k[B]$	no change	zero	1 <sup>st</sup>		$\text{s}^{-1}$	
$r = k[A]^{1/2}[B]$	$1.4 = \sqrt{2}$	$\sqrt{10} = \sqrt{2}$	1/2	1/2	$\text{M}^{1/2} \text{s}^{-1}$	

## b. Determining rate law need either

① known mechanism (13.7)

- or ② systematic variation of each reactant,  
with experimental measurement of rate
- \* each reactant, one at a time
  - \* only one reactant should vary  
(practice 13-9.1)

- General determination of "order", when  
numbers aren't simple:

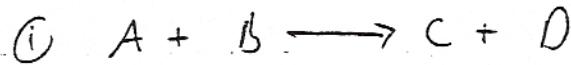
$$\text{ratio of } \frac{r_2}{r_1} = \left( \frac{[AB]_2}{[AB]_1} \right)^x \leftarrow \text{"order" for } [AB]$$

ratio of 2 concentrations

Rate effect when A is doubled; and the

<u>Rate</u>		<u>Order of [A]</u>	<u>Means</u>
doubles	$2 = 2^x$	1	$r \propto [AB]^1$
$\times 4$	$4 = 2^x$	2	$r \propto [AB]^2$
$\times 8$	$8 = 2^x$	3	$r \propto [AB]^3$
unchanged	$1 = 2^x$	0	$r \propto [AB]^0 = 1$

13-9



$[A]$   $[B]$  rate

1. 0.20 0.20 0.0078
2. 0.40 0.20 0.0156
3. 0.20 0.40 0.0078

order of A:

B:

Rate law:

$k$  (number + units):

What is rate when  $[A] = 0.80$ ,  $[B] = 0.80$



$[A]$   $[B]$  rate

0.20 0.20 0.15

0.40 0.20 0.30

0.20 0.40 0.30

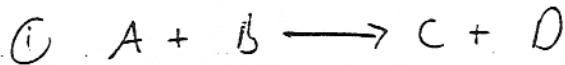
0.40 0.40 0.60

0.80 0.40 [ ]

0.80 0.80 [ ]

Rate Law:

number for  $k$ :



$[A]$      $[B]$     rate

1.	0.20	0.20	0.0078	$\xrightarrow{A \times 2 \Rightarrow \text{double rate}}$
2.	0.40	0.20	0.0156	$B \times 2 \Rightarrow \text{no rate change}$
3.	0.20	0.40	0.0078	

order of A: 1

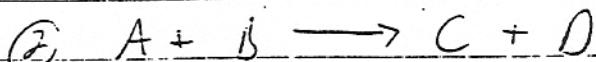
B: 0

Rate law:  $r = k[A]^1$

$$k \text{ (number + units)}: 0.0078 = k(0.20 \text{ M}) = \boxed{0.039 \text{ s}^{-1}}$$

What is rate when  $[A] = 0.80$ ,  $[B] = 0.80$

$$r = (0.039)(0.80) = \boxed{0.0312 \text{ M/s}}$$



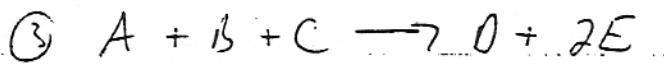
$[A]$      $[B]$     rate

0.20	0.20	0.15
0.40	0.20	0.30
0.20	0.40	0.30
0.40	0.40	0.60
0.80	0.40	1.20
0.80	0.80	2.40

Rate Law:  $r = k[A]^1[B]^1$

$$\text{number for } k: 0.15 = k(0.20)(0.20) \quad \boxed{k = 3.75 \text{ M}^{-1}\text{s}^{-1}}$$

(13-10)



$[A]$   $[B]$   $[C]$  rate

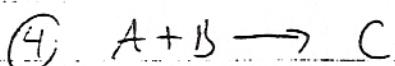
$$0.20 \quad 0.20 \quad 0.2 \quad 0.15$$

$$0.40 \quad 0.2 \quad 0.2 \quad 0.60$$

$$0.20 \quad 0.4 \quad 0.2 \quad 0.30$$

$$0.20 \quad 0.2 \quad 0.4 \quad 0.15$$

$$k =$$



$[A]$   $[B]$  rate

$$0.1 \quad 0.1 \quad 1$$

$$0.2 \quad 0.1 \quad 4$$

$$0.1 \quad 0.2 \quad 1$$

(5)  $[A]$   $[B]$  rate

$$0.1 \quad 0.1 \quad 3$$

$$0.2 \quad 0.1 \quad 6$$

$$0.1 \quad 0.2 \quad 24$$

(6)  $r = k [A][B]$

mols A mols B Liters of solvent Relative Rate

$$.5 \quad .5 \quad 1 \quad 1$$

$$.5 \quad .5 \quad 2$$

$$.5 \quad .5 \quad 0.5$$





[A]	[B]	[C]	rate	A:
0.20	0.20	0.2	0.15	$\frac{0.15}{0.15} = 1 = \left(\frac{0.2}{0.2}\right)^x$
0.40	0.2	0.2	0.60	$4 = 2^x \quad  x=2$
0.20	0.4	0.2	0.30	
0.20	0.2	0.4	0.15	

$$0.15 = k(0.2)^2(0.2)$$

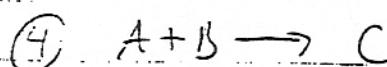
$$k = 18.75 \text{ M}^2 \text{s}^{-1}$$

$$A: \frac{0.15}{0.15} = 4 = \left(\frac{0.2}{0.2}\right)^x$$

$$4 = 2^x \quad |x=2$$

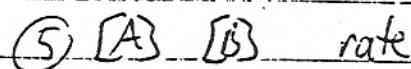
$$r = k[A]^2[B]^1[C]^0$$

$$k = \frac{0.15}{0.008}$$



[A]	[B]	rate
0.1	0.1	1
0.2	0.1	4
0.1	0.2	1

$$r = k[A]^2$$



$$r = k[A]^1[B]^3$$

A:	0.1	0.1	3
	0.2	0.1	6

$$0.1 \quad 0.2 \quad 24$$

$$b: \frac{r_2}{r_1} = \frac{24}{3} = 8 = \left(\frac{0.2}{0.1}\right)^x = 2^x$$

$$x=3$$

$$\textcircled{6} \quad r = k[A][B]$$

moles A moles B Liters of solvent Relative Rate

$$0.5 \quad 0.5 \quad 1 \quad 1$$

$$0.5 \quad 0.5 \quad 2 \quad \frac{1}{4}$$

$$0.5 \quad 0.5 \quad 0.5 \quad 4$$

both conc double

both conc  
1/2

## ① In practice

a.  $\ln 1.8 = 0.59$      $\ln \frac{100}{18} = \ln 5.56$      $\ln \frac{18}{7.2} = 0.91$   
 $= 1.7$

b.  $\ln x = 1.43$      $\ln \frac{14}{x} = 1.86$      $\ln \frac{100}{x} = 1.13$   
 $14/x = 6.42$      $100/x = 3.10$   
 $x = 4.18$      $x = 2.18$      $x = 32.3$

Assume 1<sup>st</sup> Order Rate Laws for the Following

② What is the rate constant k if [A]

goes from  $1.0 \text{ M} \rightarrow 0.32 \text{ M}$  in 46 sec?

$$\begin{aligned} kt &= \ln A_0 \\ 46 &= \ln(1/0.32) = 1.14 \\ &= \frac{1.14}{46} = 0.025 \text{ s}^{-1} \end{aligned}$$

③ If  $k = 113 \text{ years}^{-1}$ , how long will it take for 10% of A to react?

$$\begin{aligned} \text{Hint: } A_0 &= 100\% & 113t &= \ln \frac{100\%}{90\%} = -0.105 \\ A_f &= 100\% - 10\% = 90\% & & = 9.32 \times 10^{-4} \text{ years} \\ & & & = 8.1 \text{ hours} \end{aligned}$$

④ If  $k = 0.061 \text{ days}^{-1}$ , what % of a spilled poison remains after 12 days?

$$\begin{aligned} \text{Set } A_0 &= 100\% & (0.061)(12) &= \ln 100 \\ A_f &= x\% & x &= \ln 100 / 0.732 \\ & & & = 100/x \\ & & & = 98\% \end{aligned}$$

C. Half-life  $t_{1/2}$ : Time for Concentration to Drop by Half (for 1<sup>st</sup> order reaction)

$$\text{at } t_{1/2} \Rightarrow [A]_{t_{1/2}} = \frac{1}{2} [A]_0$$

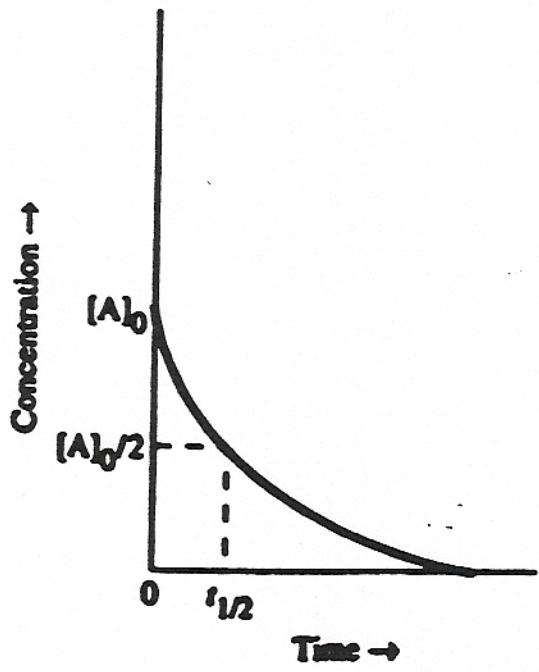
$$\rightarrow \text{so } k t_{1/2} = \ln \frac{[A]_0}{[A]_{t_{1/2}}} = \ln 2 = 0.693$$

\*  $k t_{1/2} = 0.693$

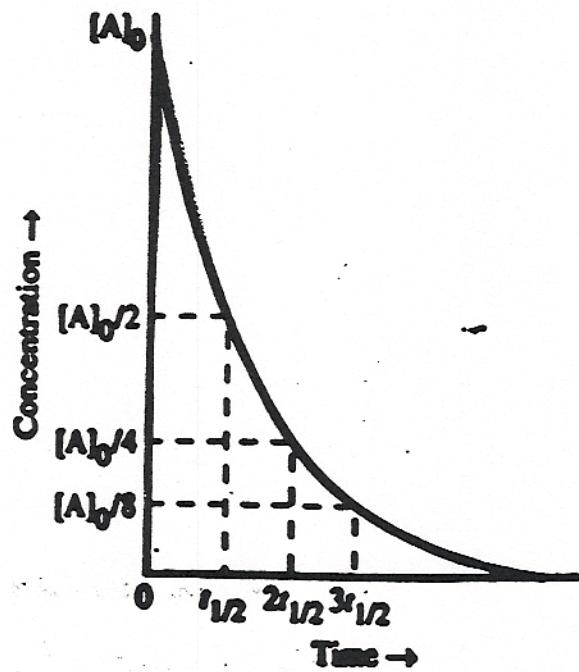
D. Higher Order Rate

- time/concentration/ $t_{1/2}$   
relationships more complex

- not responsible



(a)



(b)

**FIGURE 15.4 Half-Life of a First-Order Reaction** — The half-life is independent of the initial concentration. The initial concentration of the reactant  $[A]_0$  is less in (a) than it is in (b), but the time  $t_{1/2}$  needed for the initial concentration to decrease to half its initial value is the same. The time needed for the initial concentration to decrease to one-quarter its initial value is  $2t_{1/2}$  and to one-eighth its initial value is  $3t_{1/2}$ .

① The half-life for A is 30 sec. If you start with  $^{128}A$ , how many will be left after:

<u>t (sec)</u>	<u>Amount</u>
0	128
30	
60	
90	

<u>t(sec)</u>	<u>Amount</u>
120	
150	
180	
210	

② If  $k$  is  $0.36 \text{ days}^{-1}$ , what is  $t_{1/2}$ , and how long will it take for 75% to decay?

③  $^{14}\text{C}$  decomposes with  $t_{1/2} = 5730$  years. What is  $k$  for decomposition?

Assume 1<sup>st</sup> Order

(13-14)

- ① The half-life for A is 30 sec. If you start with 128 A, how many will be left after:

t (sec)	Amount	t (sec)	Amount
0	128	120	8
30	64	150	4
60	32	180	2
90	16	210	1

7 half-lives to hit 1%!

- ② If  $k$  is  $0.36 \text{ days}^{-1}$ , what is  $t_{1/2}$ , and how long will it take for 75% to decay?

$$kt_{1/2} = 0.693 \quad 0.36 t_{1/2} = 0.693 \quad t_{1/2} = 1.93 \text{ days}$$

$$75\% = 2 \text{ half lives}$$

$$\text{so } 2 \times 1.93 \text{ days} = \boxed{3.8 \text{ days total}}$$

$$\text{or } 36 t = \ln \frac{100\%}{75\%}$$

$$\boxed{t = 3.8 \text{ days}}$$

- ③  $^{14}\text{C}$  decomposes with  $t_{1/2} = 5730$  years. What is  $k$  for decomposition?

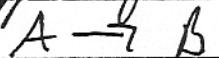
$$kt_{1/2} = 0.693 \quad k = \frac{0.693}{5730} = \boxed{1.2 \times 10^{-4} \text{ years}^{-1}}$$

## 13.4, 13.5 Reactions, Energetics, & Temp

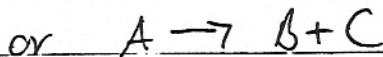
"Q: Why are rates impacted by concentrations and temp?"

### A. Nanoscale Reactions

- while an overall reaction may involve many steps (13.7), elementary steps are either unimolecular or bimolecular
- 1. Unimolecular: a single molecule either rearranges or decomposes
- energy required!



(Fig 13.7)



### 2. Bimolecular: 2 things collide

- a. orientation, angle must be suitable!

Fig 13.8      Fig 13.8

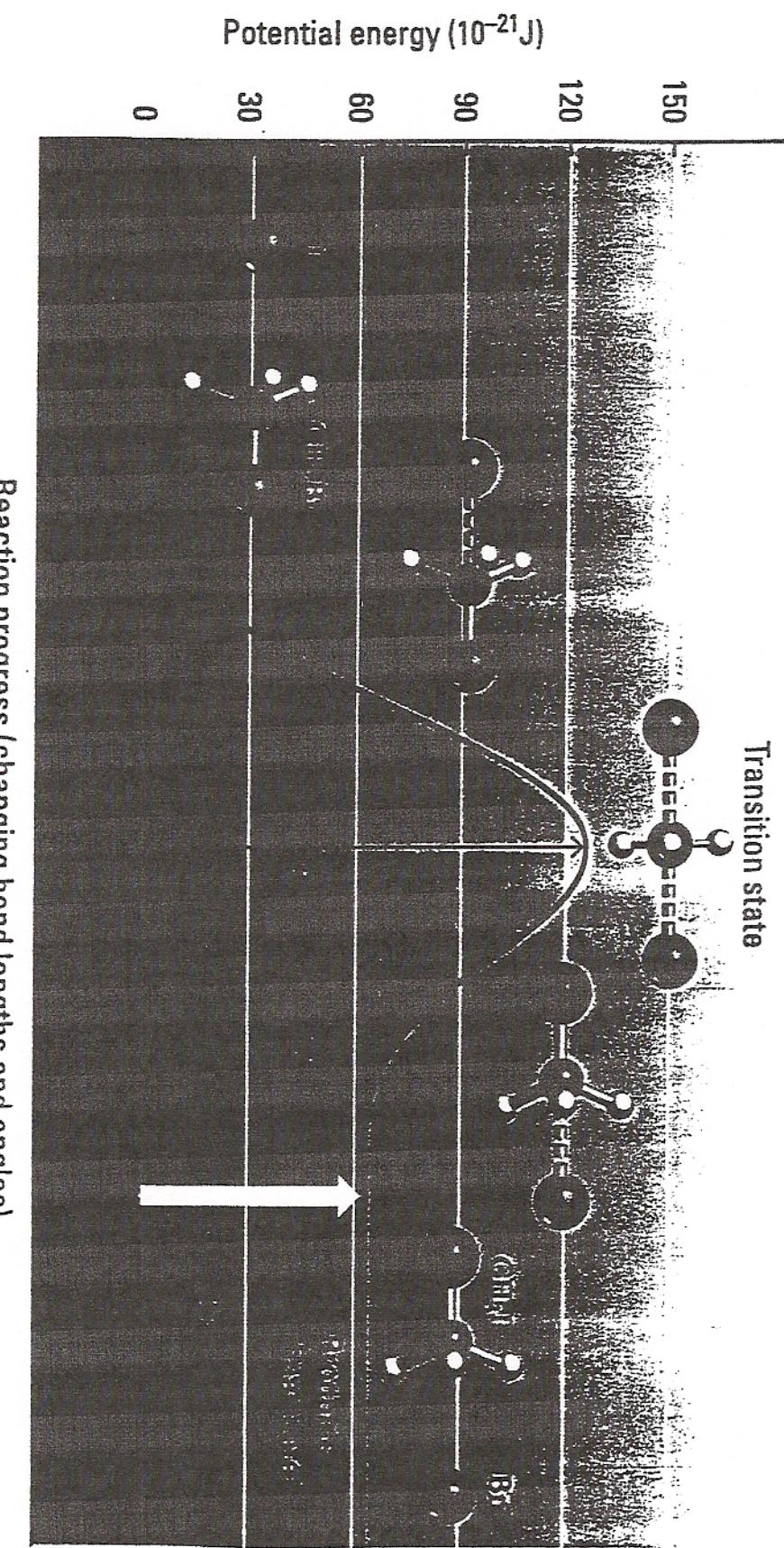
- most collisions don't succeed
- b. reactants must collide with enough energy
- called "activation energy,  $E_a$ "

higher conc  $\rightarrow$  more collisions  $\rightarrow$  faster rate Fig 13.12

higher temp  $\rightarrow$  higher energy  $\rightarrow$  more succeed

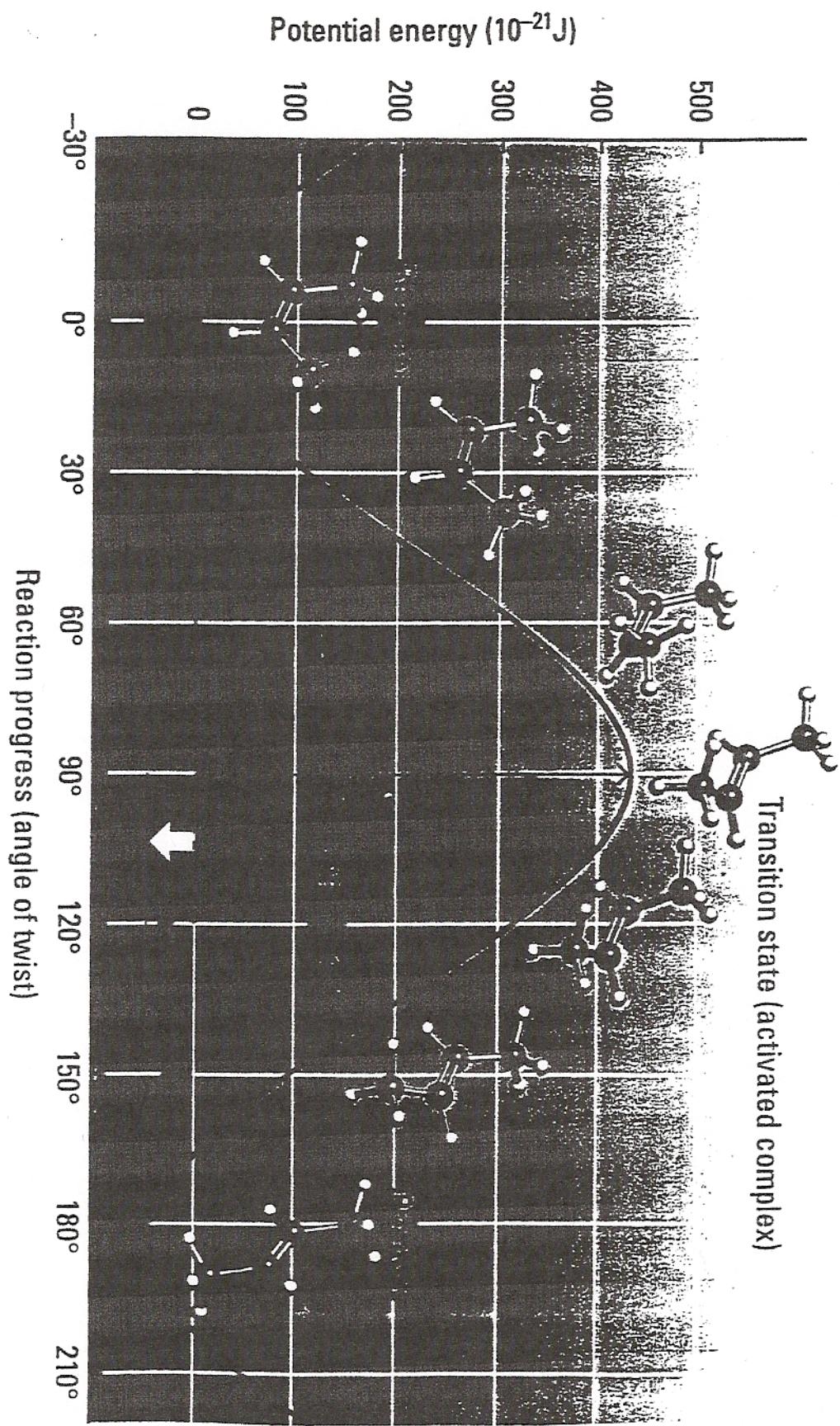
(also more collisions,

but efficiency is key)



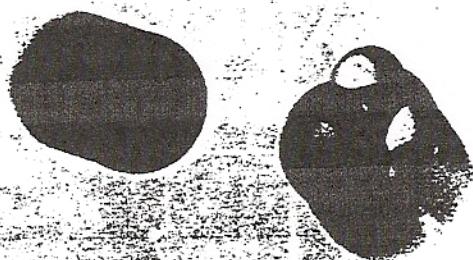
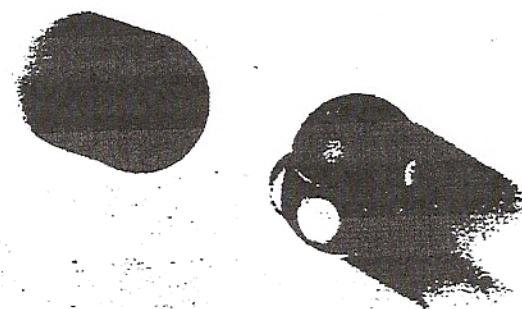
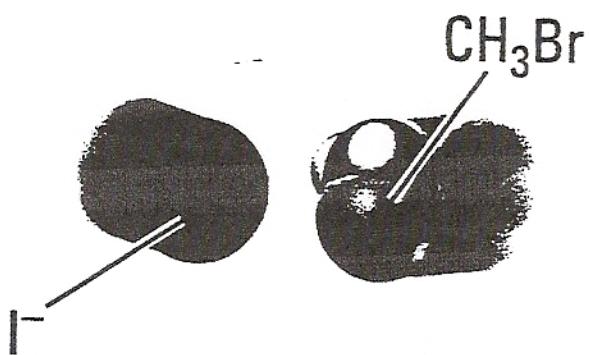
Reaction progress (changing bond lengths and angles)

Moore/Stanitski/Jurs, Chemistry: The Molecular Science  
Figure 13

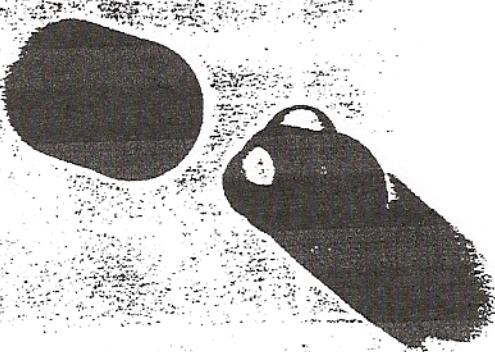


Moore/Stanitski/Jurs, Chemistry: The Molecular Science  
Figure 13.7

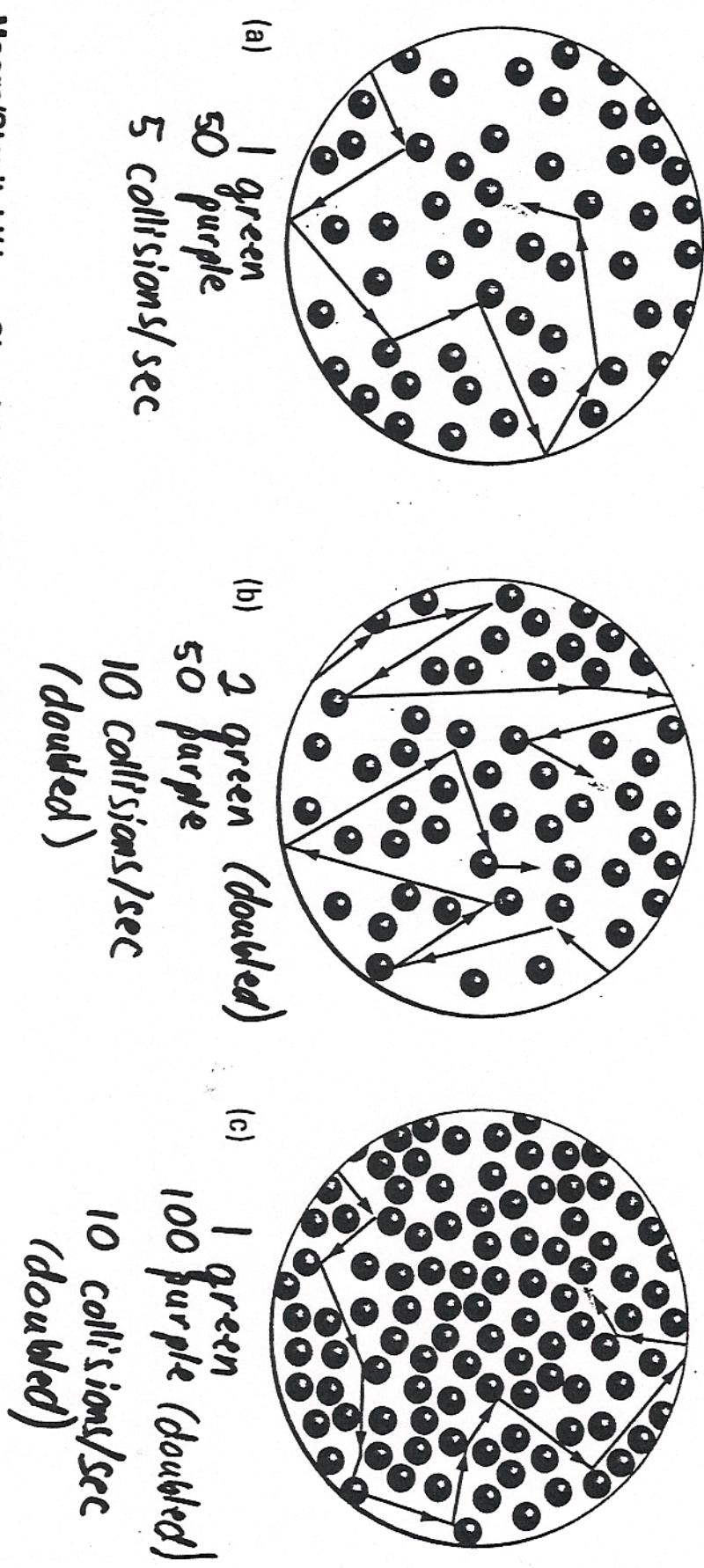
## Unsuccessful collisions



## Successful collision

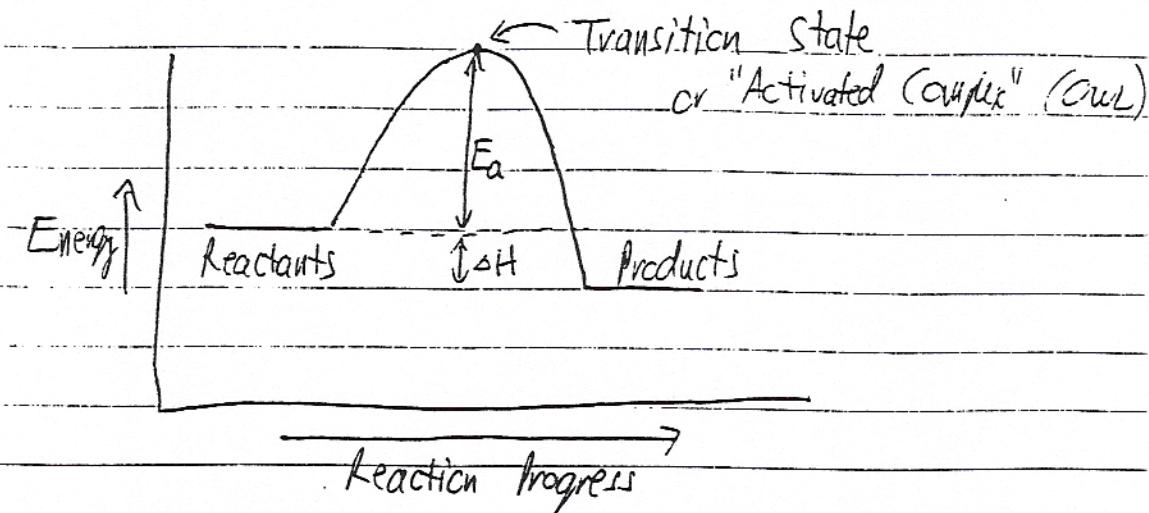


Moore/Stanitski/Jurs, Chemistry: The Molecular Science  
Unnumbered Figure 13.8



Moore/Stanski/Jurs, Chemistry: The Molecular Science  
Figure 13.12

### C. Energy Diagrams, Activation Energy, Transition State



T-state: energy max on road to products

$E_a$ : barrier

① the higher the slower!

② T-state higher than reactants or products, but must be crossed

③ even exo reactions have barrier

(because cost of breaking often precedes payoff of making)

④ higher temp  $\Rightarrow$  higher odds of clearing barrier. Greater Fraction

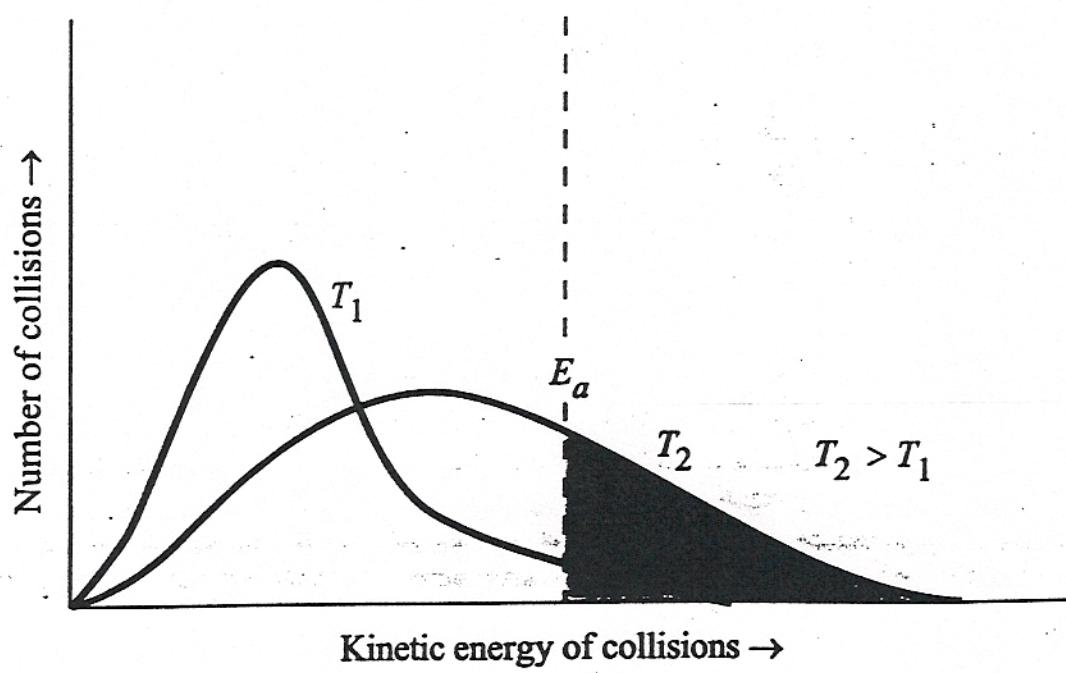
\*  $\Rightarrow k$  changes (increased) at diff. temp T 1/2, Gillespie Clear the barrier.

[Fig 15.7, Gillespie]

⑤  $E_a$  unique for each reaction  
— no correlation with  $\Delta H$ ...

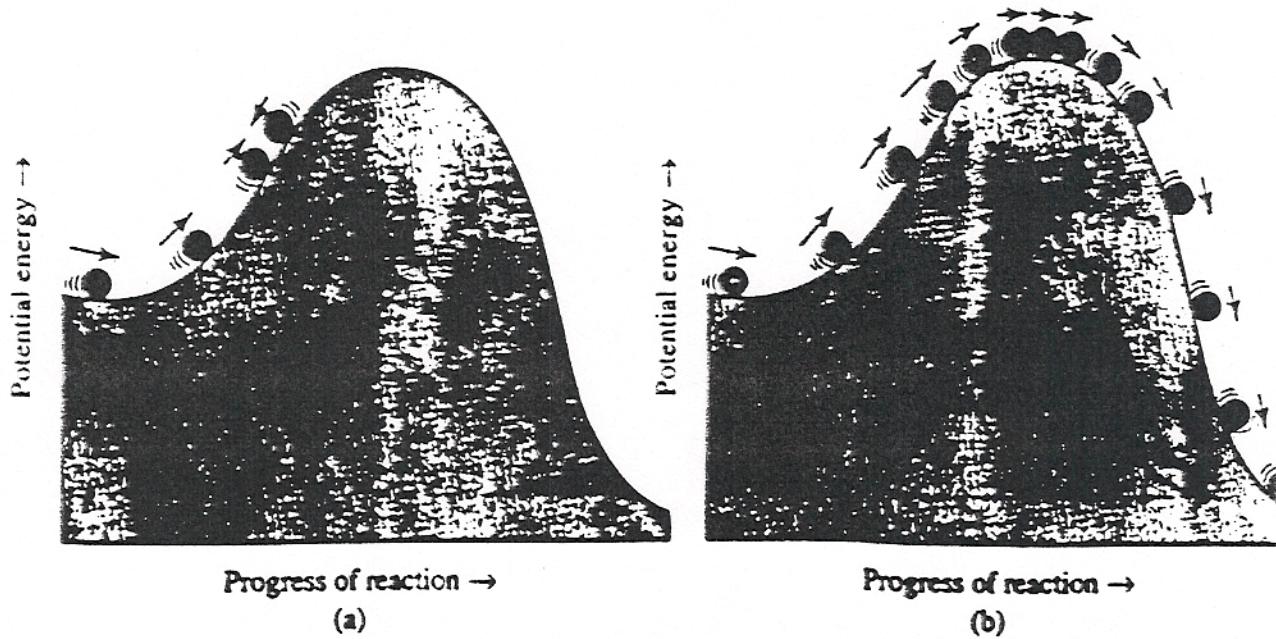
⑥ Catalysts: change mechanism ~~so~~ in such a way that T-state lowered

T 112 Fig. 15.8 Collision Energy Distributions



ATOMS MOLECULES  
AND REACTIONS  
Gillespie/Eaton/  
Humphreys/Robinson

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**FIGURE 15.7** Analogy for the Activation Energy of a Chemical Reaction  
 Energy is required to move a ball to the top of a barrier, just as energy is required for chemical reactants to form a transition state, or activated complex. (a) Here the ball has insufficient energy to climb the potential energy barrier and rolls back down the same side of the barrier. No reaction has occurred. (b) Here the ball has sufficient energy to reach the top of the potential energy barrier and may then roll down the other side. A reaction has occurred.

# A. Arrhenius Equation

$$k = A e^{-E_a/RT}$$

$R = \text{constant} = .00831$

$A = \text{constant unique}$

- complex!

to each reaction



- Qual: ① larger  $E_a \Rightarrow$  smaller  $k$
- ② higher temp  $\Rightarrow$  larger  $k$

Math: ln both sides

graphical a)  $\ln k = -\frac{E_a}{.00831} \left(\frac{1}{T}\right) + \ln A$   $y = mx + b$

solution

Graph  $k$  vs.  $1/T$ ,  
⇒ solve for  $E_a$  and  $A$

## b) 2-Point Solution

$$\ln \left( \frac{k_2}{k_1} \right) = \frac{E_a}{.00831} \left( \frac{1}{T_1} - \frac{1}{T_2} \right)$$

$E_a$  in  $\text{kJ/mole}$   
 $T$  in Kelvin

## Applications

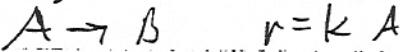
- ① Given  $k$ 's at 2 temps, can find  $E_a$
- ② Given  $E_a$  and the  $k$  at one temp, can find the  $k$  at any other
- ③ Given  $E_a$  and the  $k$  at one temp, then can find whatever temp is needed to produce a desired  $k$  ( $10$  or  $10^{+4}$  or  $10$  times faster...)

## (13.6, 7) Reaction Mechanisms & Rate Laws

### A. Examples

- elementary steps uni- or bimolecular
  - most reactions multistep (especially catalyzed ...)
  - "intermediate" - short-lived, forms in one step, destroyed in another
  - since concentrations normally too low to measure  $\Rightarrow$  \* may not appear in <sup>final</sup> rate law!! (note for multiple choice)
  - rate law should only include reactants (and catalyst)
- ~~on both sides, cancel out~~

④ rate laws of elementary steps depend directly on reactants!



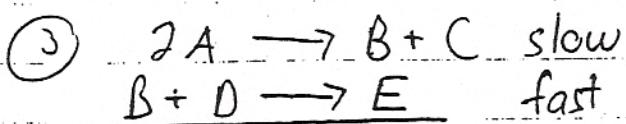
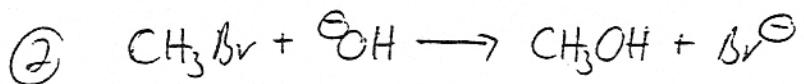
(contrast to overall balanced ...)

$\Rightarrow$  \* given mech, can deduce rate law

⑤ elementary steps must sum to give overall balanced eqn.

- handout problems

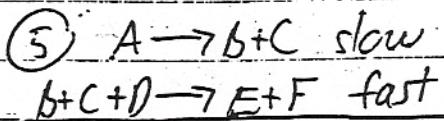
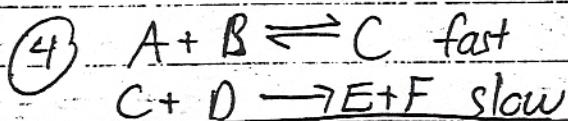
For the Following, Classify Molecularity of Elementary Steps, Identify Intermediates, and Write Overall Rate Laws



sum:

overall rate law  $r =$

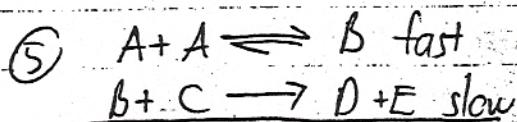
intermediate:



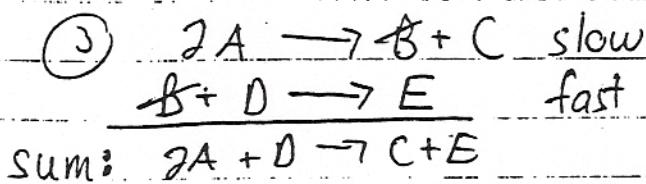
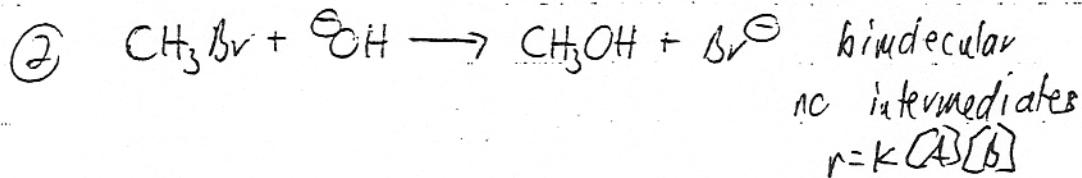
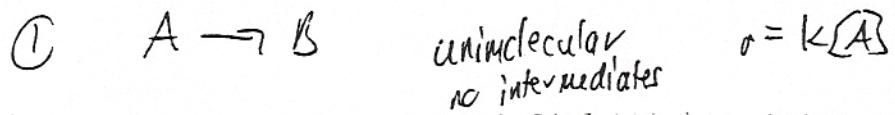
sum:

intermediate(s)

overall  $r =$

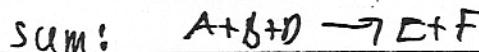
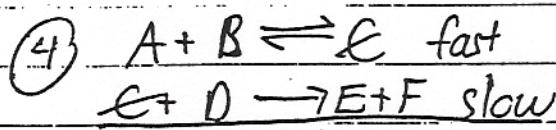


For the Following, Classify Molecularity of Elementary Steps, Identify Intermediates, and Write Overall Rate Laws



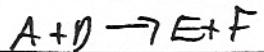
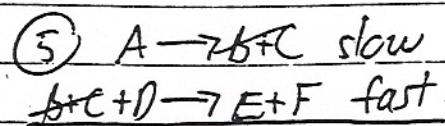
Overall rate law  $r = k[A]^2$

intermediate: B

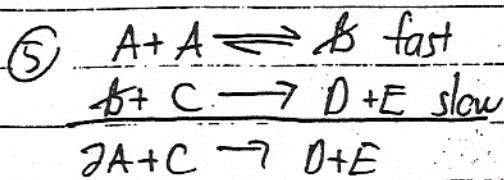


intermediate(s) C

overall  $r = k[A][B][D]$



rate =  $k[A]$



$r = k[A]^2[C]$

## B. Deducing Rate Law from Multistep

(13-20)

Mech: Determined by Slowest

Step = RATE DETERMINING STEP

- bottleneck

(I-94 Chicago; pizza in one oven bottleneck;  
Hornbacker...)

- any step after slow step has no impact on rate
- any reactant after slow step does not appear in rate law
- All reactants in or before slow step appear in rate law (overall)
  - (no intermediates allowed!!)

### Practice Problems

Skills: ① Given mech  $\Rightarrow$  write rate law

② Given rate law  $\Rightarrow$  distinguish plausible from implausible mechanisms

## Mechanisms and Rate Laws

Distinguishing among possible mechanisms, given a rate law:

1. Which mechanism is plausible for the reaction shown, given the rate law:



- a.  $A + B \rightarrow D$  (slow)  
 $D + B \rightarrow C$  (fast)
- b.  $B + B \rightarrow E$  (slow)  
 $A + E \rightarrow C$  (fast)
- c.  $A \rightarrow F$  (slow)  
 $F + B \rightarrow G$  (fast)  
 $G + B \rightarrow C$  (fast)
- d.  $B + B \rightarrow H$  (fast)  
 $A + H \rightarrow C$  (slow)

Identifying a Rate Law, given the Mechanism:

2. Given the mechanism shown, what is a reasonable rate law?



Mechanism:  $A + B \rightarrow D$  (slow)  
 $D + B \rightarrow E$  (fast)  
 $A + E \rightarrow C$  (fast)

- a.  $r = k[A][B]$
- b.  $r = k[A][E]$
- c.  $r = k[A]^2[B]^2$
- d.  $r = k[A]^2[B]^2[D][E]$

(13-21)

Chem 160-Jasperse

## Mechanisms and Rate Laws

Distinguishing among possible mechanisms, given a rate law:

1. Which mechanism is plausible for the reaction shown, given the rate law:



- a.  $A + B \rightarrow D$  (slow)  
 $D + B \rightarrow C$  (fast)

$$r = k A B$$

- b.  $B + B \rightarrow E$  (slow)  
 $A + E \rightarrow C$  (fast)

$$r = k B^2$$

- c.  $\checkmark A \rightarrow F$  (slow)  
 $F + B \rightarrow G$  (fast)  
 $G + B \rightarrow C$  (fast)

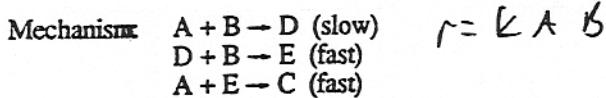
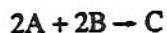
$$r = k A$$

- d.  $B + B \rightarrow H$  (fast)  
 $A + H \rightarrow C$  (slow)

$$r = k A B^2$$

Identifying a Rate Law, given the Mechanism:

2. Given the mechanism shown, what is a reasonable rate law?



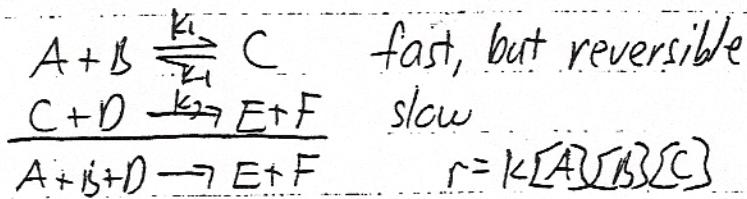
a.  $r = k[A][B]$

b.  $r = k[A][E]$

c.  $r = k[A]^2[B]^2$

d.  $r = k[A]^2[B]^2[D][E]$

# Derivation of Rate Law When 1<sup>st</sup> Step Isn't Slow



- ① Intermediates ( $C$ ) don't build up. They reach a steady state, (usually very low concentration) in which formation = destruction

$$\begin{aligned}
 &\text{rate formation} = \text{rate destruction} \\
 &k_1[A][B] = k_2[C][D]
 \end{aligned}$$

since step 2 is slow, it probably makes a small contribution to the rate of destruction and can be dropped.

$$\text{Thus } k_1[A][B] = k_2[C]$$

$$\text{Rearranged: } [C] = \frac{k_1[A][B]}{k_2}$$

$$② \text{ Overall rate given by slow step: } r = k_2[C][D]$$

$$\text{Substituting for } [C] \quad r = \frac{k_2 k_1 [A][B][D]}{k_2}$$

$$\text{since } \frac{k_2 k_1}{k_2} \text{ is itself constant, overall } r = k' [A][B][D]$$

## 13.8 Catalysts

① Increase rates

② Are themselves recycled ("catalytic converter")

- not used up, final quantity of catalyst equals initial

- used early, regenerated late in mech ("anti-intermediate")

(Fig. 13.13-15)

③ Recognition: do not appear in balanced eqn

[do] appear in rate law

④ Speed up by providing new mech with lower  $T$ -state

=  (Fig. 13.14, 13.17)

- new mech always more complex
- "tunnel" through energy barrier

⑤ While  $E_a$  reduced, overall  $\Delta H$  is unchanged!! (metabolism)

⑥ Tiny quantities suffice (because recycled)

⑦ Can reduce temp/heat requirements (metabolism)

⑧ Attraction: cost, small amounts, benefit of time, no waste ---

- industry loves them! (13.10)

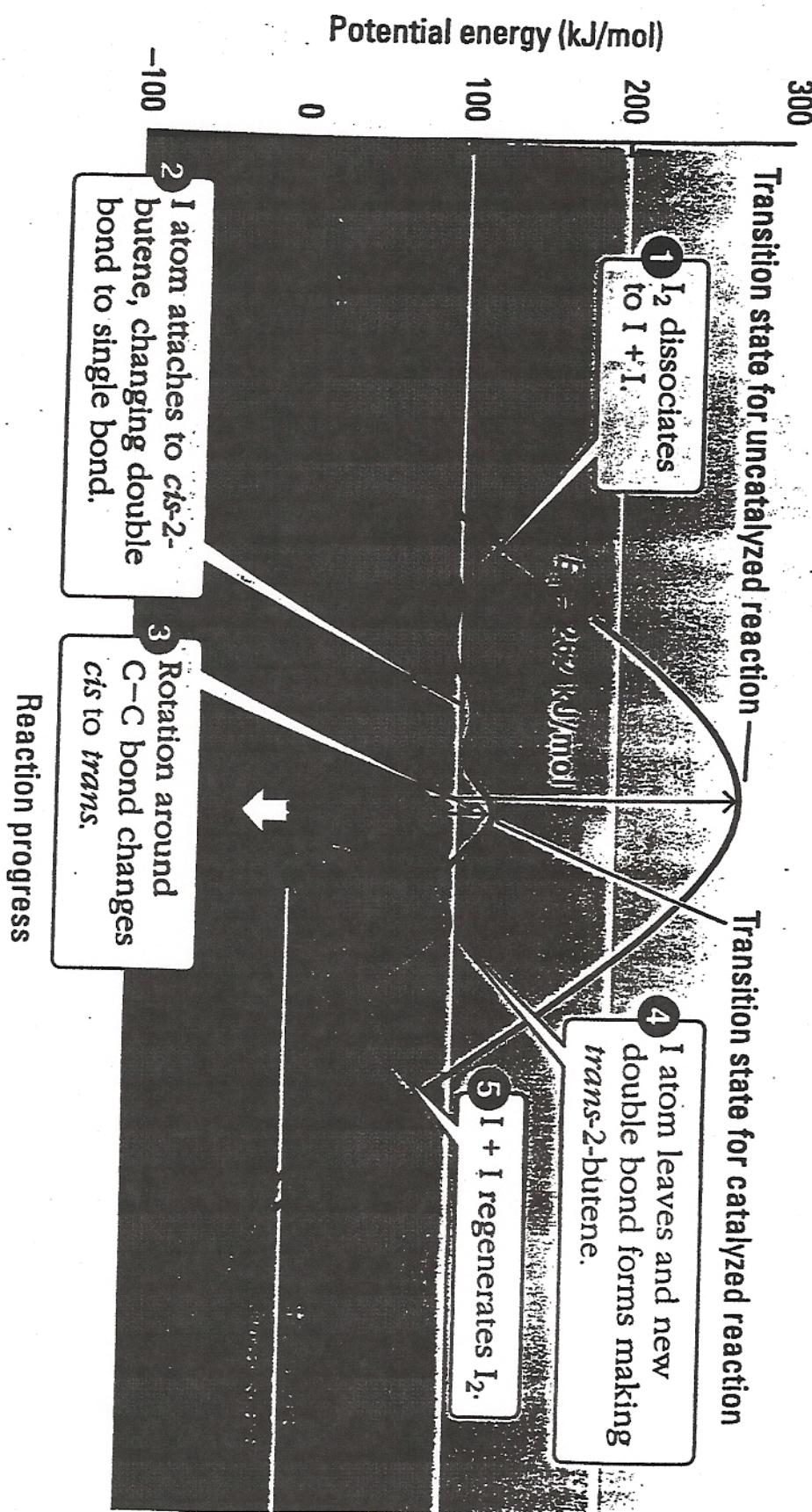
⑨ Enzyme: big proteins that Catalyze Biology (13.9)

-> 100,000 enzymes

- can increase rates by millions or billions!

- remarkable specificity

- most diseases involve enzyme malfunction, medical research addresses (on/off)



Moore/Stanski/Jurs, Chemistry: The Molecular Science  
Figure 13.14

