Optical Spectroscopy

Interaction of matter (molecules) with electromagnetic radiation ~ optical spectroscopy.

Ultraviolet-Visible

Basic facts of electromagnetic radiation (wave)

- All electromagnetic radiation can be considered as waves

Characteristics of electromagnetic waves:

- Wavelength (λ), frequency (v), wavenumber (\overline{v}) ('color' of light) - wavenumber = 1/ λ (number of waves / unit length)

Blue light ~ 400-450 nm wavelength, 25 000 – 22 222 cm $^{-1}$ Red light ~ 600-700 nm wavelength, 16 667 – 14 286 cm $^{-1}$

- Polarization: direction of transversal vibration

- linearly polarized light vs. randomly polarized

- Speed: in vacuum (n=1); c = 2.99×10^8 m/s

Considered as a particle: photon (energy packet) of energy hv.

A wave a periodic change of a *property* in space and/or time.



Basic facts of electromagnetic radiation (wave)

EM radiation as a <u>travelling</u> wave; has mutually perpendicular magnetic and electrical fields and these fields vary periodically in <u>time and space</u>.



Instantaneous snap shot of a linearly polarized $~~photon~~energy=h~\nu=\frac{hc}{\lambda}$ wave with graphic of field intensities.

Distance between two consecutive similar points along the wave (with same phase and amplitude) is λ .



 $\lambda v = c$



Electromagnetic radiation covers a large energy range

Animation of a pencil of polarized light.

Polarization of light: electromagnetic wave is a transverse wave which has both an electric and a magnetic component.

View a polarized electromagnetic wave traveling towards you, Then you would observe the amplitude variation of the wave in one plane – polarized light – plane of polarization.



<u>Natural light</u>: consists of pencils of light with planes of polarization in <u>all possible directions</u>.





Polarizers: Planes of polarization parallel



Light Passing Through Crossed Polarizers



http://www.olympusmicro.com/primer/lightandcolor/polarization.html

Polarization of Light http://www.olympusmicro.com/primer/java/polarizedlight/filters/index.html

Polarization of Light (3-D Version) http://www.olympusmicro.com/primer/java/polarizedlight/3dpolarized/index.html



http://www.olympusmicro.com/primer/java/polarizedlight/filters/index.html

The energy (E) of a molecule consists of translational, rotational, vibrational and electronic energy (major terms).

E_{molecule} = E_{nuclearspin} + E_{electronspin} + E_{translational} +E_{rotation} +E_{vibration} +E_{electronic}

Translation – movement of the molecule through space Spin – nuclear and electron spin

Rotational - rotation of the molecule

Vibrational – vibration of the atoms with respect to each other Electronic – mutual interactions of the electrons and nuclei

All these energy states (stationary states) are quantized except translational energy.

Quantized states have precisely assigned energy values.



In molecules electrons reside molecular orbitals, $\sigma,\,\pi,\,\sigma^{\star},\,\pi^{\star}$ and non-bonding orbitals



For any covalent bonding orbital in a molecule there is a corresponding anti-bonding orbital of higher energy.



The difference in energy between molecular bonding, non-bonding and anti-bonding orbitals ranges from 125-650 kJ/mole

Electronic energy levels and transitions



Each electronic state is associated with a set of vibrational states; and each vibrational state is associated with a set of rotational states.

The energy differences between rotational and vibrational levels are much smaller.



Relative energy values in different domains



 $E_{molecule} = E_{rotation} + E_{vibration} + E_{electronic}$





Covalent molecules: Bonding involves molecular orbitals.

Electrons are in molecular orbitals $\sigma,\pi,\delta,...$ and lone pairs (generally many molecular orbitals exist, most important here HOMO and LUMO).

In addition $\sigma^*, \pi^*, \delta^*, ...$ (anti-bonding molecular orbitals are formed).

Most molecules in ground state have electron spins paired, no net spin, singlet states.



Relative energy values in different domains: ground state HOMO orbital



 $E_{molecule} = +E_{rotation} +E_{vibration} +E_{electronic}$

Ground State Molecular Orbitals of molecules: Chromophores



Photon and molecule interactions

When electromagnetic radiation (photon) 'interacts' with a molecule, scattering or absorption occurs at the outset.

Types of scattering:

Elastic – all energy of the colliding photon is preserved, wavelength of light remains unaltered (Rayleigh scattering – elastic scattering).

Stokes: Raman – some energy is lost as vibrational energy of The molecule, emitted photon wavelength is longer than the original wavelength of the photon. Inelastic scattering.

Anti-Stokes: Raman – emitted photon has shorter wavelength than the original. Inelastic scattering.

Photon and molecule interactions: Absorption

In an absorption event, a single photon of light is fully absorbed by a single molecule; energy of the molecule is increased by the energy of the photon.

$\Delta E = h v$

h = Plank's constant

- The high energy molecule relaxes by processes:

- i. non-radiative heat
- ii. radiative fluorescence
 - phosphorescence

$_$ stimulated emission

 leads to changes in molecular structure/chemical reaction – e.g. *Photosynthesis*



UV-VIS Spectroscopy

Photons in the region of UV-VIS are of energy comparable to energy required for transitions between electronic states.

UV-VIS absorption arises from electronic transitions.

Atoms \rightarrow molecules : atomic orbitals \rightarrow molecular orbitals Electronic transitions \leftrightarrow molecular orbitals.

lons, complexes \rightarrow d-d transitions and/or charge transfer complexes (internal redox reaction)

The difference in energy between bonding, non-bonding and anti-bonding orbitals ranges from 125-650 kJ/mol; corresponds to EM radiation in UV 100-350nm, and VIS 350-700nm.

Light absorption changes the charge distribution of electrons of the molecule.







 $\label{eq:conjugation: Spreading of π-MOs over the molecular} framework. Leads to$ *narrowing* $of HOMO-LUMO gap. Increases λ_{max}- bathochromic effect.}$









n-electron conjugation: $n \rightarrow \pi^*$





Photon energy, frequency and wavelength relationships

 $\Delta E_1 > \Delta E_2 > \Delta E_3 > \Delta E_4$ $v_1 > v_2 > v_3 > v_4$ $\lambda_1 < \lambda_2 < \lambda_3 < \lambda_4$



Intramolecular charge transfer transitions absorbs radiation in the electronic spectra.













Condensed phase spectra do not have much fine structure due to significant line broadening.

Gas phase UV-VIS spectra has fine structure.



Lambert-Beer Law: Derivation

A beam of monochromatic light falling on an absorbing and homogeneous medium loses the intensity of the beam (Power, P) as it traverses through the medium. The loss of the power of the beam, dP, for a traveled path length, dx, is proportional to the concentration of the absorbing species, power of the beam and the length dx. dx



 $dP\alpha$ Pcdx

 $A_{\lambda} = \varepsilon_{\lambda} / c$

$$\frac{dP}{P} = -\beta cdx$$

Integrating within limits;

$$\int \frac{dP}{P} = -\int \beta cdx \implies \int_{P_0}^{P_{out}} \frac{dP}{P} = -\int_0^b \beta cdx \quad which is \ln \frac{P_{out}}{P_0} = -\beta bc$$

$$2.303 \log_{10} \frac{P_{out}}{P_0} = -\beta bc \qquad \log_{10} \frac{P_0}{P_{out}} = \frac{\beta bc}{2.303} = \varepsilon bc \quad A = \varepsilon bc$$

$$A_\lambda = \varepsilon_\lambda bc$$

$$\int \frac{P_{out}}{P_0} dP_0 = \frac{\beta bc}{2.303} = \varepsilon bc \quad A = \varepsilon bc$$

Absorbance is directly proportional to c.



$$\begin{split} T &= \frac{P_{out}}{P_0} \\ \%T &= \frac{P_{out}}{P_0} \times 100 \\ A &= log \bigg(\frac{P_0}{P_{out}} \bigg) \\ A &= -log_{10}(T) = log_{10} \bigg(\frac{1}{T} \bigg) \end{split}$$

molar absorptivities vary by orders of magnitude: 10⁴-10⁶ are termed *high intensity absorptions* 10³-10⁴ are termed *low intensity absorptions* 0 to 10³ are the absorptions of *forbidden transitions*



Calibration curve:



Absorption of a molecule is usually characterized by its molar absorptivity.

$$\begin{split} \epsilon_\lambda &= \text{absorbance of a solution of unit concentration in} \\ \text{a unit path length at wavelength } \lambda. \\ \text{It is a measure of the transition probability.} \end{split}$$

For mixtures absorbing at the same λ ;

A_λ=Σ ε_{λ,i}bc_i



Single beam spectrometer:







Xenon lamp emission spectrum



UV-VIS Sources:



A monochromator configuration:



Fastie-Ebert Configuration







Non-linearity of calibration curve: Instrumentation effect Slit width





Band width ~ physical slit width

A range of wave lengths (more than one, for sure) enters the sample - polychromatic beam.

Monochromator Band Width

Rays exiting the monochromator is strictly <u>not</u> monochromatic. Only <u>nearly monochromatic</u>, has a wavelength distribution around (band width) λ , commonly referred to as monochromatic radiation wavelength. The smaller the band width (FWHM) of the beam, the better is the system.



Non monochromatic radiation leads calibration plots to deviate from linearity. Illustration:

For a 'monochromatic' beam λ ,

$log (P_o/P) = A = \varepsilon bc = kc$ $P_o/P = 10^{\varepsilon bc}$	(11) (12)	
Similarly, at λ ', P _o /P'= 10 ^{ε'bc}	(13)	

The radiant power of two wavelengths passing through the solvent is given by $P_o + P'_o$, and that passing through the solution containing absorbing species by P + P'.



The combined absorbance is

 $A_{c} = \log \left[(P_{o} + P'_{o}) / (P + P') \right]$ (14)

Substituting for P and P', we obtain; $A_c = \log \left[(P_o + P'_o) / (P_o 10^{-cbc} + P'_o 10^{-c'bc}) \right]$ (15)

Non-linearity arises <u>because molar absorptivity is different</u> for the two wavelengths; seen clearly at high c values.

$$\begin{aligned} P_{out} &= (P_0 10^{-\epsilon bc} + P_0^{'} 10^{-\epsilon^{c} bc}) \\ P_{in} &= (P_0 + P_0^{'}) \\ P_{out} &\neq P_{in} 10^{-k bc} \quad \text{not in the Beer's Law form} \quad P_{out} &= P_{in} 10^{-\epsilon bc} \end{aligned}$$

The combined absorbance is

$$A_{c} = \log [(P_{o} + P'_{o})/(P + P')]$$

Substituting for P and P', we obtain; $A_c = \log \left[(P_o + P'_o) / (P_o \cdot 10^{-sbc} + P'_o \cdot 10^{-s'bc}) \right]$ (15)

Non-linearity arises <u>because molar absorptivity is different</u> <u>for the two wavelengths</u>.

(14)





Substituting for P and P', we obtain;

$$A_c = \log \left[(P_o + P'_o) / (P_o \ 10^{-cbc} + P'_o \ 10^{-c'bc}) \right]$$
 (15)

If molar absorptivity is the same for the two wavelengths;

$$P_{out} = (P_0 10^{-\epsilon bc} + P_0' 10^{-\epsilon' bc})$$

$$P_{in} = (P_0 + P_0') 10^{-\epsilon bc} \quad (if \ \epsilon = \epsilon')$$

$$P_{out} = P_{in} 10^{-\epsilon bc} \quad the Beer's Law form !!$$

Detector Response

<u>The dynamic range</u> of a detector is that concentration range over which a concentration dependent output is produced.

The minimum of the range will be the concentration at which the output is at the detection limit and the maximum that concentration where the detector no longer responds to a concentration increase.

The dynamic range is usually given as a concentration ratio and is thus, dimensionless.

The linear dynamic range of a detector is that concentration range over which the detector output is linearly related to solute concentration.









Resolution: ~ Ability to distinguish consecutive peaks.



Monochromator bandwidth is directly related to the slit widths in addition to grating characteristics.



Turning the grating around it's center allows "different monochromatic λ " s to leave the exit slit of monochromator.







Energy maximum for λ diffracted such that $\alpha\text{=}\beta.$

http://www.shimadzu.com/products/opt/oh80jt0000001uz0.html



Angular Dispersion of Gratings

Dispersion is a 'measure' of the angle the grating must be rotated to change wavelength of the the exiting light by a unit wavelength.

i.e. angular separation $d\varphi$ obtained for two wavelengths separated by $d\lambda.$

$$\frac{\Delta\phi}{\Delta\lambda} = \frac{\mathsf{n}}{\mathsf{d}\cos\phi}$$

Smaller d values of the grating generate larger dispersions leading to higher resolutions.



Rays exiting the monochromator is strictly not monochromatic. Only *nearly monochromatic*, has a wavelength distribution around (band width) λ , commonly referred to as monochromatic radiation wavelength. The smaller the band width (FWHM) of the beam, the better is the system.





When a monochromator is set to a particular wavelength, light with a Gaussian intensity distribution of wavelengths emerges from the exit slit. The heavy black line represents the distribution of light that reaches the sample. The spectral bandwidth is defined as the FWHM.

Spectral slit width is defined as the total spread of wavelengths represented by the blue lines.

The spectral bandwidth will always be narrower than the spectral slit width.



Two consecutive peaks with $\Delta\lambda$ having a valley of 5% are said to be resolved peaks.

$$R = \frac{\lambda}{\Lambda \lambda} = nN$$

Resolution

Resolution is defined as the ability of an instrument to separate light into finite, distinct wavelength regions and distinguish these finite regions from each other. It is primarily governed by the physical slit width of the instrument.

 $\mathsf{R} = \frac{\lambda}{\Delta \lambda} = \mathsf{n}\mathsf{N}$

n = order N= # grooves illuminated

The above in combination with the inherent angular dispersion of light from the exit of the monochromator to the detector of the instrument determines resolution.

Spectral resolution is a measure of the ability of an instrument to differentiate between two adjacent wavelengths λ and $\lambda+\Delta\lambda.$









Note: uneven response



Diodes (semiconductor)

-SI-SI-SI-SI-SI-SI-
-Si-Si-Si-Si-Si-Si-
Si-Si-Si-Si-Si-Si-
Si-Si-Si-Si-Si-Si-

Si Crystal





http://www.allaboutcircuits.com/vol_3/chpt_2/4.html

Detectors:

Diodes (semiconductor)

-Si-Si-Si-Si-Si- -Si-Si-Si-Si-Si-Si- Si-Si-Si-Si-Si-Si- 	-Si-Si-Si-Si-Si-Si- -Si-P-Si-Si-Si-Si- Si-Si-Si-Si-Si-Si-Si-	-Si-Si-Si-Si-Si-Si- -Si-Si-Si-Si-Si-Si- Si-Ga®Si-Si-Si-Si-
Si-Si-Si-Si-Si-Si-	Si-Si-Si-Si-Si-Si-	Si-Si-Si-Si-Si-Si-

Si Crystal

n-type Si

p-type Si

Detectors:

-Si-Si-Si-Si-Si-Si-	
-Si-P-Si-Si-Si-Si-	•
Si-Si-Si-Si-Si-Si-	
Śi-Śi-Śi-Śi-Śi-Śi-	

n-type Si



n-type Si





Foward bias i ≠ 0



Reverse bias i = 0



Reverse bias

Current (signal) produced is proportional number of photons falling (i.e. intensity of light) at the junction.





Diode-Array Spectrophotometer



Double Beam Spectrophotometer



Optical system of a double-beam spectrophotometer

UV-VIS in Quantitative Analysis

Inherently UV-VIS absorbing species Organic chromophores, transition metal ions oxoanions, elemental halogens.

Non-absorbing species may be converted to absorbing species quantitatively.

 $\begin{array}{l} \mathsf{Fe}^{+3} + \mathsf{SCN}^{\scriptscriptstyle -} \to \mathsf{Fe}\mathsf{SCN}^{+2} \\ \mathsf{Cr}^{+3} \to \mathsf{CrO}_4^{-2} \\ \mathsf{Ni}^{+2} \to \mathsf{Ni}\text{-}\mathsf{DMG} \\ \mathsf{Pb}^{+2} \to \mathsf{Pb}\text{-}\mathsf{Diphenyl-thiocarbazone} \end{array}$

General Procedure (Single species)

- a. select a λ most sensitive/less susceptible to slight drifts in λ (better reproducibility).
- b. choose the solvent (medium) to disperse the 'test' and standards.

solvent, pH, temperature, ionic strength and interferents. c. matched cells (clean, scratch less, dust free)

d. generate a *calibration curve* (A vs. c) : A = mc + b

If media of 'tests' and standards are not comparable it is best to use standard addition method, not the *calibration curve* for quantitation.

Solvent Effects:

The color exhibited by a solute and/or the intensity of the peaks may vary with the nature of the solvent in which the chromophore is dissolved in.



Solvent Effects:



Note: In general much more than the polarity of the solvent molecules is involved in solvent effects (solvatochromism) leading to wavelength shifts.

Solvent Effects:



Standard Addition Method







v

V

Standard Addition Method (one addition):

$$\begin{split} A_{0} &= kvc_{u} / V \\ A_{1} &= k(vc_{u} + v_{s}c_{s}) / V \\ \frac{A_{0}}{A_{1}} &= \frac{vc_{u}}{vc_{u} + v_{s}c_{s}} \end{split}$$

Solve for c_u.





Advantages of Spectrophotometric Titration:

- 1. Calculations based on multiple measurements, minimizes errors.
- 2. Change of Absorbance is monitored, interferents do not contribute to the final calculation..



3. Extrapolation: to determine equivalence point. Reactions with relatively low K can be analyzed.



4. Successive titrations possible. e.g. Bi+2, Cu+2, vs EDTA.

K_{Bi-EDTA}> K_{Cu-EDTA}

@745nm



Standard Addition Method (modification)

Series of standards prepared Mix standards with unknown; Unknown volume = volume of standard = v ml







Derivative Spectroscopy

First or higher derivatives of absorbance with respect to wavelength for qualitative analysis and for quantification.

$$\begin{split} \mathsf{A} &= \mathsf{f}(\lambda) & \text{zeroth order} \\ \frac{\mathsf{d}\mathsf{A}}{\mathsf{d}\lambda} &= \mathsf{f}'(\lambda) & \text{first order} \\ \frac{\mathsf{d}^2\mathsf{A}}{\mathsf{d}\lambda^2} &= \mathsf{f}''(\lambda) & \text{second order} \end{split}$$





Resolution enhancement

qualitative analysis: to identify the presence of two analytes with Very similar λ_{max} values that are not resolved in the absorbance spectrum.





Jobs Method: Empirical Formula of binary compounds/complexes using the *method of continuous variation* or Jobs Method.

$\mathbf{P} + \mathbf{X} = \mathbf{P}_n \mathbf{X}_m$

The amount of one of the components is varied from a small value to a large value while the amount of the other component is varied from large to small. The amount of the product formed is monitored via the absorbance of the product.

aP + bX = dD

P + kX = mD

k=b/a m= d/a

If a series of solutions is made, each containing the <u>same</u> <u>total number of moles</u> of P and X, <u>but a different ratio</u>, R = moles P/moles X, the maximum amount of product, D, is obtained in the solution in which R = k (the stoichiometric ratio).

When R > k, there is an excess of reagent X, so reagent P is the limiting reagent and X is in excess.

when R < k, there is an excess of reagent P, and X is limiting reagent and P is the limiting reagent.



Isobestic Point:

 $A \leftrightarrow B$ (Both absorb, generate spectra.) $A = B + H^+$

This term is usually employed with reference to a set of absorption spectra, plotted on the same chart for a set of solutions in which the <u>sum of the concentrations</u> of two principal absorbing components, <u>A and B, is constant</u>.

The curves of absorbance against wavelength (or frequency) for such a set of mixtures often all intersect at one or more points, called isobestic points.





Molar absorptivity of A and B same at isobestic point.

Isosbestic points are commonly met when electronic spectra are taken;

(a) on a solution in which a chemical reaction is in progress (in which case the two absorbing components concerned are a 'reactant' and a 'product'),

or (b) on a solution in which the two absorbing components are in equilibrium and their relative proportions are controlled by the concentration of some other component,

$$A \rightleftharpoons B + H^+$$

In all these examples, A (and/or B) may be coming from a single *chemical species* or a mixture of chemical species present in invariant proportion.



Evidence of an intermediate of a reaction.

If absorption spectra of the types considered above intersect at many isosbestic points, this is *prima facie evidence* in case;

(a) for the formation of a *reaction intermediate* in substantial concentration, $A \rightarrow B \rightarrow C$

$$A \to B \to C$$

(b) for the involvement of a third absorbing species in the equilibrium, e.g. $% \left({{{\mathbf{x}}_{i}}_{i}} \right)$

$$A \rightleftharpoons B + H^+ \rightleftharpoons C + 2H^+$$